

# Type-Directed Language Extension for Effectful Computations

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## ABSTRACT

Computation types such as functors, applicative functors and monads have become common abstractions for modeling effectful computations in functional programming languages. They are often used together with special language extensions intended to simplify the syntax of monadic expressions. We can simplify it even more by employing types rather than just mechanical syntactic transformation.

In this paper we present `scala-workflow`, a macro-based extension to the Scala programming language that offers uniform syntax for structuring effectful computations expressed as abstract interfaces with a stackable set of combinators. Unlike similar syntactic extensions, such as `F#`'s computation expressions, Haskell's `do`-notation and Scala's own `for`-expressions, `scala-workflow` allows users to transparently blend pure and effectful functions in a bounded context, as they are separated during macro expansion based on the types of subexpressions.

## Categories and Subject Descriptors

D.3.2 [Programming languages]: Language Classification — Applicative (functional) languages; D.3.3 [Language Constructs and Features]: Control structures

## General Terms

Languages, Algorithms

## Keywords

Scala, macros, effects, monads, functors

## 1. INTRODUCTION

Programs that involve effectful aspects of computation, like non-determinism, concurrency, exceptions or IO, invite programming languages to seek appropriate abstractions that can capture them. Some languages prefer to have built-in

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single-purpose primitives. Others, and most notably functional ones, employ a variety of generic algebraic structures capable of expressing computational effects.

The concept of monads, originally introduced in the context of computations by Moggi [16] gained significant attention in the Haskell community and became the de-facto standard way of structuring computations with effects in Haskell [29]. McBride and Paterson introduced applicative functors [15] (also known as *sequences* or *idioms*), that are weaker than monads, but are more widespread. Both monads and idioms are supersets of functors [11], however the latter are rarely used as effectful containers.

An entirely different approach to effectful computations are type and effect systems [25]. In the context of Scala there is ongoing work [22] on lightweight encoding of effect-polymorphic function types in Scala annotations.

To facilitate effectful computations, functional programming languages provide special extensions, aimed to simplify the syntax of the application of effectful combinators. The main idea underneath most of them is to extend the language with special syntactic forms, that are mechanically rewritten into calls of effectful combinators.

In this paper we present `scala-workflow`, a syntactic extension for the Scala programming language, available for download at <https://github.com/aztek/scala-workflow>. Unlike most similar extensions in other programming languages, `scala-workflow` does not simply expand the expression according to syntax-driven transformation rules, but employs type information of subexpressions to direct the rewriting process. Ultimately, `scala-workflow` allows users to transparently blend effectful and pure computations, which otherwise would require manual separation and more boilerplate code.

To illustrate this approach, let us give an example of composition of asynchronous computations built with Scala's `concurrent.Future` class. Here, two potentially slow computations `F()` and `G(x: Int)`, producing integers, are placed inside the future call to create future objects.

```
val f: Future[Int] = future { F() }  
def g(x: Int): Future[Int] = future { G(x) }
```

With `scala-workflow` the arithmetic expression that combines the results of `f` and `g` can be expressed in direct style. The result is a future object that waits for the execution of `f`, supplies its incremented value to `g` and doubles the result.

```
context [Future] {  
  $(2 * g(f + 1))  
}
```

The arithmetic expression is put inside the `$` macro that bounds the scope of rewriting and the context declaration that specifies the type of computational effect. Whereas addition and multiplication, applied to future objects, do not type check in ordinary Scala, they are correctly used with our extension, because the macro expansion takes place before the type checking. The produced well-typed expression uses calls to methods `bind` and `map` of the object `future_` that implements the treatment of effects similarly to `Future`'s own `flatMap` and `map`.

```
future_.bind(
  (x$1: Int) =>
    future_.map(
      (x$2: Int) =>
        2 * x$2
      )(g(x$1 + 1))
)(f)
```

The `$` macro notation is different from the usual way of expressing composition of futures in Scala with `for-comprehension`, as illustrated by the snippet below.

```
for {
  x ← f
  y ← g(x + 1)
} yield 2 * y
```

Note that one has to separate monadic bindings from pure multiplication and name intermediate results, which was not needed with `scala-workflow`.

Unlike `for`-notation, `scala-workflow` is not tied to monads. An elaborate rewriting algorithm enables uniform syntax for different computation types. For example, applicative functors receive syntactic support with the same `$` macro as long as the expression inside does not require handling effects that exceed their capabilities. The next snippet produces a stream, built by summing elements standing on the same position in streams `xs`, `ys` and `zs`, using `zipStream`, Scala's counterpart of Haskell's `zipList` idiom.

```
context(zipStream) {
  $(xs + ys + zs)
}
```

The fitness of the computation type is checked statically and the rewriting algorithm always rewrites the expression in a way that requires the least powerful computation type sufficient to express the computation.

In what follows, we first describe related work in Section 2. Section 3 overviews the main features of `scala-workflow`. Next, a number of use cases are detailed in Section 4. Section 5 addresses further improvements and Section 6 concludes the paper.

## 2. RELATED WORK

Perhaps the most famous syntactic extension for monadic computations is Haskell's `do`-notation [12]. It is based on mechanical translation of monadic bindings within a `do` block into calls of monadic `>>=` and `>>`. Pure and effectful bindings end up syntactically separated, as the former are defined explicitly as `let`-expressions.

The `do`-notation influenced similar syntactic extensions in other programming languages, such as `perform`-notation in OCaml [5] or `let!`-notation in Common Lisp [23]. Scala

provides its counterpart known as `for`-expressions [17]. The principal idea remains the same, however Scala supports more versatile syntax and therefore employs a variety of combinators, such as `map`, `flatMap`, `withFilter` and `foreach`. Due to the lack of a built-in interface for monads in Scala, `for`-expressions expect an object to implement methods with appropriate names and types. Again, pure bindings are syntactically distinguished from effectful ones.

A generalization of the list comprehension syntax [27], known as `monad comprehension` [28] is available in Haskell. It allows to shrink multiple monadic bindings into a one-line expression, that can further be refined with projection and grouping functions. This can be a better alternative to `do`-notation for certain applications [8].

Together with the original definition of idiom, the notation of idiom brackets was introduced. They essentially unclutter the syntax of application of pure function to effectful arguments. Idiom brackets are now available in Idris [2] and Strathclyde Haskell Enhancement [14]. A proposal<sup>1</sup> has been made to add support for applicative syntax resembling `do`-notation to GHC. `scala-workflow` trivially supports idiom brackets by implementing a more general notation.

Petricek and Syme proposed a more elaborate approach to effectful syntax [20]. Their result, called *computation expression*, is available as part of the F# programming language [19]. The idea behind it is to extend the syntax of the language with effectful counterparts of some of the keywords, such as `let`, `return` and `yield` (correspondingly, `let!`, `return!` and `yield!`) and use them to demarcate effectful computations in a context, bounded by the scope of a *computation builder*. The content of the bounds is then translated, again in a purely syntactic manner, to calls of builder methods. What makes this approach more refined is that the builder is merely a stackable set of methods, that mirror the features of the language (for example, `While` method for loops, `TryWith` for exceptions and `Delay` for lazy computations). We borrow this idea in `scala-workflow` to a certain extent, but put it in a setting where no extension of the host language is needed.

A macro-based approach to the implementation of a syntactic extension for asynchronous computations has been taken in `async` [9] by Haller and Zaugg. The code is put inside the `async` macro call with the `await` function call denoting asynchronous subexpressions. Crockett's *effectful* [6] library generalizes this approach to arbitrary monads. The approach taken in `scala-workflow` essentially allows to get rid of explicit annotations of effectful subexpressions by inferring them automatically during macro expansion. Both `async` and *effectful*, however, support wider subset of language features of Scala, allowed in the annotated block of code, including conditional expressions, loops and pattern matching.

A somewhat generalized translation, discriminating pure from effectful expressions, was implemented in Scala's extension for delimited continuations [21]. It employs selective CPS transformation driven by type and effect system based on `@cps` type annotations. Effectful monadic computations can be expressed in direct style with this framework, provided that the user reflects monadic values explicitly by passing continuations to underlying `bind` operations. The translation procedure, presented in this work, employs a

<sup>1</sup><https://ghc.haskell.org/trac/ghc/wiki/ApplicativeDo>

similar style of type-directed transformation, however, is driven by effectful type constructors, marking effectful expressions, rather than type annotations. This approach enables less boilerplate, but loses type safety of the input code.

Swamy et al. [24] introduced the type-directed extension to ML for monadic programming. This work implements a similar technique for Scala, but additionally employs special analysis of dependencies between effectful expressions that enables support of the whole hierarchy of computation types rather than just monads.

### 3. OVERVIEW

The implementation of `scala-workflow` is built with Scala’s compiler-time macro system. Shortly after its inception in 2012 [4], it has proved [3] to be a productive infrastructure for a number of programming techniques, such as language virtualization, deeply embedded DSLs and boilerplate generation. `scala-workflow` employs *untyped macros*, one of the macro flavors of the Macro Paradise<sup>2</sup> project. This approach is different from extensions to other languages, commonly implemented at the compiler level, and allowed us to obtain a modular and extensible implementation.

The main language feature, provided by the library is *workflow brackets*, syntactically represented as `$` macro function. The code that is put inside the brackets is freed from the boilerplate, needed for the treatment of effects, while keeping its logical structure. This freedom allows it not to pass type checking in Scala. The macro inserts all the necessary combinators and expands into correct code.

#### 3.1 Hierarchy of workflows

The key concept of `scala-workflow` is a *workflow*, that is a structure that collects features of computation types. All workflows are instances of the `Workflow[F[_]]` trait where `F[_]` is a type constructor that encodes an effect produced during a computation. The `Workflow[F[_]]` trait itself does not provide any methods and is merely an initial point of extension with new methods coming from derived traits. It is the calls of these methods that get inserted during rewriting of the expression inside the workflow brackets. Every method added to the `Workflow[F[_]]` corresponds to a language feature that can be used in the expression.

Currently `scala-workflow` supports four traits, that extend the base trait. All of them make different kinds of interplay between effectful computations admissible inside the brackets.

Method `point` enables the brackets not to contain any effectful computations at all. In such case the expression inside the brackets simply becomes the argument of `point`. Note, that `point` corresponds to Haskell’s monadic `return` and applicative `pure`.

```
trait Pointing[F[_]] extends Workflow[F] {
  def point[A](a: => A): F[A]
}
```

As a running example, consider the workflow instance `option` of type `Workflow[Option]` that treats the partial nature of computations with `Option` as effect.

Thus, the expression such as `$(42)` gets rewritten into `option.point(42)`, because `42` is a value, and thus a pure expression.

<sup>2</sup><http://docs.scala-lang.org/overviews/macros/paradise.html>

Method `map` enables the brackets to contain exactly one effectful expression. As the name suggests, this method corresponds to a functor’s `map`.

```
trait Mapping[F[_]] extends Workflow[F] {
  def map[A, B](f: A => B): F[A] => F[B]
}
```

In the context of the `option` workflow, a safe floating point division function `divide` can be seen as an effectful computation.

```
def divide(x: Double, y: Double): Option[Double] =
  if (y == 0) None else Some(x / y)
```

To safely calculate an expression, such as  $1 + \frac{n}{m}$  for any  $n$  and  $m$ , one can simply write `$(1 + divide(n, m))`. The implementation of `option` propagates the effect of the absence of return value when  $m = 0$ , so that the whole expression would be evaluated to `None` in such case. The produced expression is the following one.

```
option.map(
  (x$1: Double) =>
    1 + x$1
)(divide(n, m))
```

An expression with more than one effectful subexpression, such as `divide(n, m) + divide(p, q)`, can not appear inside the brackets of a workflow that only implements `map`.

Method `app`, however, allows the brackets to contain an arbitrary positive number of *independent* effectful expressions. It is a generalization of `map`, therefore `Applying` extends `Mapping`. It corresponds to Haskell’s applicative `<*>` operator.

```
trait Applying[F[_]] extends Workflow[F]
  with Mapping[F] {
  def app[A, B](f: F[A] => B): F[A] => F[B]
}
```

Generally speaking, `Applying` is capable of lifting [10] the application of a pure function over effectful arguments. Thus, the expression `$(divide(n, m) + divide(p, q))` can be rewritten with a combination of `app` and `map`.

```
option.app(
  option.map(
    (x$1: Int) => (x$2: Int) =>
      x$1 + x$2
  )(divide(n, m))
)(divide(p, q))
```

To illustrate the concept of dependence between effectful computations, consider an expression `divide(divide(n, m), k)`. Here, the result of the outermost `divide` can only be obtained after the result of the innermost `divide` is known and computational effect during its execution has been treated. This was not the case with the previous examples, where the order of evaluation of effectful expressions was not specified. Methods `app` and `map` are not capable of expressing this kind of structured evaluation.

Finally, method `bind` enables the brackets to contain a pair of dependent effectful expressions. It corresponds to Haskell’s `>>=` and Scala’s `flatMap`.

```
trait Binding[F[_]] extends Workflow[F] {
  def bind[A, B](f: A => F[B]): F[A] => F[B]
}
```

Nested divide calls are allowed in a workflow with bind.

```
option.bind(
  (x$1: Double) =>
    divide(x$1, k)
)(divide(n, m))
```

It is of course easy to compose more common abstractions of a functor, an idiom and a monad by mixing traits with appropriate methods, effectively forming a hierarchy of these structures. `scala-workflow` elaborates on it slightly more by adding *semigroupoids* to the picture. This is a concept, much like functors and monads, borrowed from category theory [1]. Informally, *semi-monads* and *semi-idioms* are respectively monads and idioms without the point method.

```
trait Functor[F[_]] extends Mapping[F]

trait SemiIdiom[F[_]] extends Functor[F]
  with Applying[F]

trait Idiom[F[_]] extends SemiIdiom[F]
  with Pointing[F] {
  def map[A, B](f: A => B) = app(point(f))
}

trait SemiMonad[F[_]] extends SemiIdiom[F]
  with Binding[F]

trait Monad[F[_]] extends Idiom[F]
  with Binding[F] {
  def app[A, B](f: F[A => B]) =
    bind(a => bind((g: A => B) => point(g(a)))(f))
}
```

Note that we are able to provide default implementations for `map` in `Idiom` and both `map` and `app` in `Monad`. Using these aliases we can define workflows in the same manner we would have defined idioms and monads in other functional languages. The example below illustrates possible implementation of `option`.

```
val option = new Monad[Option] {
  def point[A](a: => A) = Option(a)
  def bind[A, B](f: A => Option[B]) = {
    case Some(a) => f(a)
    case None => None
  }
}
```

The important thing from the `scala-workflow` perspective, however, is that the `option` instance has methods `point`, `map` and `app` (that is, it implements correspondent traits, mixed to `Workflow[Option]`), because this is what will be checked during expression rewriting.

### 3.2 Context declaration

While workflow brackets scope the bounds of expression rewriting, a *context declaration* scopes the bounds of workflow instance application.

A context declaration is a macro context, that tells workflow brackets inside of it which workflow instance will provide methods, generated after expression rewriting. The first argument of `context` is either a workflow instance explicitly, or a type constructor, such that there is a workflow

instance available in the implicit scope. The second argument is an expression, where all workflow brackets will be rewritten to method calls of the declared workflow instance.

To trigger rewriting of the expression in the brackets, the example from the previous section should be put inside context declaration.

```
context(option) {
  $(1 + divide(n, m))
}
```

`scala-workflow` is shipped with a library of workflow instances for commonly used classes, including that of type `Workflow[Option]`. Moreover, most of the instances are defined with the `implicit` keyword. The following snippet summons `option` from the implicit scope and is equivalent to the previous one.

```
context[Option] {
  $(1 + divide(n, m))
}
```

In some cases the whole body of `context` is directly a block of code put in the workflow brackets. Alias macro `workflow` is defined specifically for that. Similarly to `context` it takes either the workflow instance object or the type constructor reference. Once again, the following snippet is equivalent to the previous ones.

```
workflow[Option] {
  1 + divide(n, m)
}
```

The choice between the `context` and the `workflow` is entirely up to the user. Examples in Section 4 feature both declarations.

### 3.3 Expression rewriting

Translation of the expression inside the `$` macro into calls of workflow methods is done in two stages. First, the bindings elimination algorithm replaces all effectful subexpressions inside the expression with synthetic unique identifiers, building the graph of dependencies between subexpressions along the way. Then the rewriting algorithm generates appropriate workflow method calls based on the number and connection between collected effectful bindings.

The bindings elimination algorithm works with a given expression in a given workflow context. It takes the untyped syntax tree of the expression (it might not necessarily type check in regular Scala) and produces a graph of variable bindings together with a type-correct expression modulo the absence of effects. Steps of the algorithm:

1. Traverse nodes of the syntax tree in post-order (sub-nodes are visited before the root). The initial scope of effectful bindings is empty.
2. While visiting the node, check its type in the lexical scope of bindings. If the type corresponds to the type of the effect in the given workflow context (that is, it is `F[A]` for some `A` in the context `Workflow[F[_]]`), generate a unique identifier, save the binding between identifier and the node and replace the node with the identifier reference. Otherwise, leave the node as it is.
3. Traverse the outermost nodes until the top level of the expression is reached.

As a working example consider a computation in the option workflow, that, as discussed previously, can be expressed with methods map and app.

```
workflow(option) {
  2 * divide(1, 3) + 4 * divide(5, 6)
}
```

The binding elimination algorithm starts with the leaves, numbers in this case. All of them are of type Int, so it continues. Type checking divide(1, 3) returns the type Option[Double], that corresponds to the effectful type constructor Option. The newly created identifier x\$1 has the type Double and points to the expression divide(1, 2). The rewritten expression 2 \* x\$1 has the type Double. In the same way, divide(5, 6) yields the new binding x\$2 of the type Double. The rewritten expression 4 \* x\$2 has the type Double and so does the whole expression altogether. The result of the algorithm is a partially rewritten expression and a table of bindings.

```
2 * x$1 + 4 * x$2
```

Id	Type	Body
x\$1	Double	divide(1, 3)
x\$2	Double	divide(5, 6)

The synthetic variables are independent: x\$1 does not appear in the body of x\$2 and x\$2 does not appear in the body of x\$1. The rewriting algorithm then produces a combination of methods appropriate to express the computation, app and map in this case.

```
option.app(
  option.map(
    (x$1: Int) => (x$2: Int) =>
      2 * x$1 + 4 * x$2
  )(divide(5, 6))
)(divide(1, 3))
```

In the second example consider a snippet of code in the option workflow that involves the result of one effectful computation that is needed for another one. It requires option to support bind and map to rewrite this expression.

```
workflow(option) {
  2 * divide(divide(3, 4), 5)
}
```

The binding elimination algorithm type checks the numbers first, then generates the new identifier x\$1 of type Double for the node divide(3, 4). Type checking the expression divide(x\$1, 5) returns Option[Double], which produces another binding x\$2. Eventually, the whole partially rewritten expression type checks to Double.

```
2 * x$2
```

Id	Type	Body
x\$1	Double	divide(2, 3)
x\$2	Double	divide(x\$1, 4)

Note that this time x\$2 depends on x\$1, in order to evaluate x\$2 we have to evaluate x\$1 first. The notion of dependency between effectful expressions requires the bind operator and the rewriting algorithm produces a combination of bind and map.

```
option.map(
  (x$2: Double) =>
    2 * x$2
)(option.bind(
  (x$1: Int) =>
    divide(x$1, 5)
)(divide(3, 4)))
```

The rewriting algorithm is limited to the language features of Scala admissible inside the expression. The currently supported subset includes atomic values, function applications and blocks of val-expressions.

The translation of the expression consists of a series of type checking and rewritings. Should there be a type error during the translation, scala-workflow aborts the compilation and tries to present the error clearly and with sufficient detail. As an example, the snippet below mistakenly multiplies a string by a number. A type error occurs when two bindings are eliminated, leaving the expression partially rewritten.

```
workflow(option) {
  "2" * divide(divide(3, 4), 5)
}
```

The error message presents the expression that failed to type check, all the bindings, their types and the expressions they point to.

```
error: type mismatch;
found   : Double
required: Int
    "2"$.times(x$2)

where

  x$1: Double <- divide(3, 4)
  x$2: Double <- divide(x$1, 5)
```

Type error during rewriting of expression within Option context

```
workflow(option) {
  ~
```

### 3.4 Composition of workflows

It is usually the case that type constructor F[\_] encodes a single effect produced by a computation. Multiple effects can be expressed with composition of effectful type constructors. At the same time, expressing composition of workflows might not be an easy task.

Syntactically, scala-workflow provides the binary operator \$ as a uniform notion for composition of workflows. That is, if f is Workflow[F[\_]] and g is Workflow[G[\_]], f \$ g is Workflow[F[G[\_]]]<sup>3</sup>.

However, composition of workflows requires knowledge about their structure, therefore the \$ operator is defined separately for every computation type rather than generally in the Workflow[\_] trait.

Composition of functors is separated from the interface of a functor and defined in the FunctorComposition trait, that is mixed to the Functor trait.

<sup>3</sup>Hereinafter, the notation for composition of type constructors is deliberately shortened for typographical reasons. The correct notation would use *type level λ-function* and in this case would be {**type** λ[α] = Workflow[F[G[α]]]}#λ.

```

trait FunctorComposition[F[_]] { f: Functor[F] =>
  def $ [G[_]](g: Functor[G]) =
    new Functor[F[G[_]]] {
      def map[A, B](h: A => B) = f map (g map h)
    }
  def & [G[_]](g: Functor[G]) = g $ this
}

```

Method `&` behaves as `$` with the arguments flipped. For any functors `f` and `g`, `f $ g` is equivalent to `g & f`.

Traits `SemiIdiomComposition` and `IdiomComposition` are defined in the same way. The fact that functors, semi-idioms and idioms form a hierarchy has a pleasant side effect here. It is possible to compose workflows of different classes; the resulting workflow will implement the weaker class of the two. The dynamic dispatch mechanism in Scala guarantees to choose the method from the right trait. For example, if `f` is `Functor[F[_]]` and `g` is `Idiom[G[_]]`, `f $ g` becomes `Functor[F[G[_]]]`, since functors are weaker than idioms.

While it is possible to provide a generic implementation for composition of pairs of functors, semi-idioms and idioms, no such implementation exists for pairs of arbitrary semi-monads and monads. A common strategy in the latter case employs monad transformers [13]. To maintain a uniform syntax of workflow composition we would like, in a similar manner, to define the `MonadComposition` trait, providing methods `$` and `&`. The implementation of one of these methods would work as a monad transformer. However, some transformers, such as `StateT`, do not build a direct composition of type constructors and therefore cannot be expressed in this notation. In such cases composition must be expressed manually using a different operator.

Most monads only have a transformer for one of the methods `$` and `&`. For that reason, `scala-workflow` refines the interface of monad composition by introducing the notion of *left-composable* and *right-composable* monads.

`LeftMonad[F[_]]` denotes a monad, capable of providing an implementation of the `$` method. Its counterpart `RightMonad[F[_]]` provides the `&` method.

```

trait LeftMonad[F[_]] extends Monad[F] {
  def $ [G[_]](g: Monad[G]): Monad[F[G[_]]]
  override def $ [G[_]](g: RightMonad[G]) =
    $(g.asInstanceOf[Monad[G]])
}
trait RightMonad[F[_]] extends Monad[F] {
  def & [G[_]](g: Monad[G]): Monad[G[F[_]]]
  override def & [G[_]](g: LeftMonad[G]) =
    &(g.asInstanceOf[Monad[G]])
}

```

The definition of a monad that supports composition is done in one place, implementation of the monad transformer is provided as part of the interface. For example, `reader[E]` and `accumulator[M]` workflows (counterparts of Haskell's `Reader` and `Writer` monads) are defined as `LeftMonad` and `RightMonad` correspondingly.

Finally, the `MonadComposition` trait implements methods `$` and `&`, provided that the argument is a monad, capable to compose or be composed.

```

trait MonadComposition[F[_]] { f: Monad[F] =>
  def $ [G[_]](g: RightMonad[G]) = g & this
  def & [G[_]](g: LeftMonad[G]) = g $ this
}

```

For every two monads `f` and `g`, composition `f $ g` is a monad only when either `f` is left-composable or `g` is right-composable. Similarly, `f & g` is a monad when `f` is right-composable or `g` is left-composable.

The exact same notion of left- and right-composability is implemented for semi-monads.

Once again, the hierarchy of functors, idioms and monads allows to compose workflows of all these classes using the same syntax. The resulting workflow will implement the weaker interface of the two operands. As an example, consider the composition of the workflow `map[T]`, that captures computations over values of hash maps with keys of type `T` and `option`. While `option` implements `RightMonad`, `map[T]` is only a functor, so composition `map[String] $ option` is a functor as well. It corresponds to the type constructor `Map[String, Option[_]]`.

## 4. USE CASES

We argue that `scala-workflow` can assist in a number of applications. In this section we present a series of case studies, employing features of the extension.

### 4.1 Boilerplate elimination

Following the example given in [15] for idiom brackets, we present an enhanced implementation of an evaluator for a language of expressions, that abstracts the variable environment and the propagation of failure of environment lookup.

The definition of the abstract syntax of expressions with variables and addition is given as an algebraic data type.

```

sealed trait Expr
case class Var(id: String) extends Expr
case class Val(value: Int) extends Expr
case class Add(lhs: Expr, rhs: Expr) extends Expr

```

Variables are fetched from the environment of type `Env`. Function `fetch` looks up a variable in the environment and either returns an integer or fails, which is encoded as a value of type `Option[Int]`.

```

type Env = Map[String, Int]
def fetch(x: String)(env: Env) = env.get(x)

```

The evaluator of the expression in the given environment is simply a function of type `Expr => Env => Option[Int]`.

```

def eval(expr: Expr)(env: Env): Option[Int] =
  expr match {
    case Var(x) => fetch(x)(env)
    case Val(n) => Some(n)
    case Add(x, y) => for {
      lhs <- eval(x)(env)
      rhs <- eval(y)(env)
    } yield lhs + rhs
  }

```

This implementation can be improved. Note, that one has to explicitly pass the environment around and to have rather awkward syntax to propagate failure in the `Add` case. Both concerns can be addressed by encapsulation the boilerplate in an appropriate workflow. Here function `[A]` represents a workflow of a function with a fixed argument of type `A`, equivalent to Haskell's `(a ->)` monad. We compose function `[Env]` and `option` to build a workflow for type constructor `Env => Option[_]`.

The body of the function can now be put inside context declaration.

```
def eval: Expr => Env => Option[Int] =
  context(function[Env] $ option) {
    case Var(x) => fetch(x)
    case Val(n) => $(n)
    case Add(x, y) => $(eval(x) + eval(y))
  }
```

This new notation enables separation of concerns between evaluation strategy, environment handling and failure propagation, as the latter two are hidden in the implementation of corresponding workflow objects. This effectively reduces the amount of boilerplate code in this example.

## 4.2 Domain-specific languages

scala-workflow can be used as a syntactic enhancement for embedded domain-specific languages. In this example, it assists a simple framework for demand-driven functional reactive programming [7].

The Cell trait defines a unit of data, that can be assigned with := and fetched with !. Cells can depend on each others values, much like they do in spreadsheets.

```
trait Cell[T] {
  def ! : T
  def := (value: T)
}
```

Cell has an instance of Idiom, such that point creates a source cell, that stores a value and allows to change it and app creates an observer cell, that takes the value of some other cell to compute its own. Reassigning observer cells does not make sense, hence the exception.

```
val frp = new Idiom[Cell] {
  def point[A](a: => A) = new Cell[A] {
    private var value = a
    def := (a: A) { value = a }
    def ! = value
  }
  def app[A, B](f: Cell[A => B]) =
    a => new Cell[B] {
      def ! = f!(a!)
      def := (value: T) {
        throw new UnsupportedOperationException
      }
    }
}
```

A value, independent of values of any cells, put inside \$, will be translated to point and effectively act as a source cell, whereas an expression that combines values of cells becomes an observer cell.

```
context(frp) {
  val a = $(10)
  val b = $(5)
  val c = $(a + b * 2)
  println(c!)
  b := 7
  println(c!)
}
```

Dereferencing a cell makes it reevaluate the whole tree of dependent cells. The snippet above will print 20 and 24.

## 4.3 Transparent exception handling

Consider an example of a program that parses XML document fetched from the web. Each step of the program can end in an error. The provided address might not be a valid URL, we might not be able to fetch the page over the network or the contents of the page might not be correct XML. One way to implement these failing functions is through the use of exceptions, that guarantee that the execution will not go further than the point of the error.

```
def fetchXML(address: String): XML = {
  val url = URL.fromString(address)
  val page = Page.fetch(url)
  val contents = page.getContents
  XML.fromString(contents)
}
```

Unlike Java, Scala does not support checked exceptions, therefore the compiler is unable to distinguish between functions that do and do not throw exceptions (in other words, effectful and pure). Following the spirit of statically typed functional programming, one might want to promote the effect of the exception to the type level. For that reason Scala 2.10 offers the scala.util.Try monad, that stores either the result of a computation or a Throwable object that represents a failure. Achieving the lofty goal of making exception effects explicit, however, stumbles on the syntactic awkwardness of monadic exception handling.

In the following snippet, effectful methods URL.fromString, Page.fetch and XML.fromString are assumed to return values wrapped in Try instead of throwing an exception.

```
def fetchXML(address: String): Try[XML] =
  for {
    url ← URL.fromString(address)
    page ← Page.fetch(url)
    contents = page.getContents
    xml ← XML.fromString(contents)
  } yield xml
```

It takes more than just a syntactic transformation to handle Try. One has to inspect the types of val expressions to separate effectful binds from pure values assignments and insert either ← or = operators. Moreover, one has to excessively name the intermediate results of the computation.

Putting the code in the workflow[Try] context makes the code syntactically equivalent to its exception-based version.

```
def fetchXML(address: String): Try[XML] =
  workflow[Try] {
    val url = URL.fromString(address)
    val page = Page.fetch(url)
    val contents = page.getContents
    XML.fromString(contents)
  }
```

The workflow definition workflow[Try] syntactically resembles try keyword. One can further apply Try's recover method to mirror the whole try/catch expression. The result of the function, however, would still be wrapped in Try.

## 4.4 Imperative functional programming

Programs in functional languages can gain clarity with imperative syntax using scala-workflow. This example shows how computations, interspersed with logging can be expressed in a purely functional manner and at the same

time have the same syntactical structure as imperative code with log writes as side effects.

We represent logging as a workflow for type constructor `(_, List[String])`, where the first argument of the pair is the result of a computation and the second one is a list of log messages. A built-in implementation of such workflow is `accumulator[M]`. It is similar to Haskell's `Writer` monad.

```
val logging = accumulator[List[String]]
```

Every function that intends to write to a log inside a logging workflow should produce a pair of the result value and a list of messages, generated during its computation.

```
def mult(x: Int, y: Int) =  
  (x * y, List(s"Calculating $x * $y"))
```

A function that does not perform any computation and simply writes to the log has the type `(Unit, List[String])`.

```
def info(message: String) = (Unit, List(message))
```

Now, wrapping the code in a logging workflow allows to intersperse pure and effectful functions.

```
val (result, log) = workflow(logging) {  
  info("Assigning x to 2")  
  val x = 2  
  info("We are about to multiply by 3")  
  val triple = mult(3, x)  
  info("We are about to calculate something complex")  
  val cube = mult(mult(x, x), x)  
  val sum = cube + triple  
  info("Actually, only half of it was needed")  
  sum / 2  
}
```

The outcome of the evaluation is a pair of the result value 7 and the accumulated list of log messages.

```
List("Assigning x to 2",  
      "We are about to multiply by 3",  
      "Calculating 3 * 2",  
      "We are about to calculate something complex",  
      "Calculating 2 * 2",  
      "Calculating 4 * 2",  
      "Actually, only half of it was needed")
```

Note, that we got imperative-looking code implemented in a purely functional subset of the language. No mutable state or side effects were involved in this example.

## 5. FUTURE WORK

There is a number of directions, where `scala-workflow` can be further improved. They are left for future work.

**Up-to-date implementation.** As it was mentioned before, the current implementation of `scala-workflow` employs untyped macros. Their distinctive feature is that the macro expansion is performed before type checking, which is crucial for the type-driven algorithm. Unfortunately for us, untyped macros were discontinued<sup>4</sup> and are no longer supported in Macro Paradise. A sensible replacement should be *macro annotations*, that are also expanded before type checking. However, being on the cutting edge of Macro Paradise development, they are not mature enough to support

<sup>4</sup><http://scalamacros.org/news/2013/08/05/macro-paradise-2.0.0-snapshot.html>

`scala-workflow` as of now. Specifically, there are problems with visibility of declarations from the current scope of the macro, that present an obstacle for the implementation. They are expected to be solved in the future.<sup>5</sup>

An annotation-based implementation will replace context and workflow macros with synonymous annotation macros.

```
@workflow[List] val x = List(1, 2) * List(4, 5)
```

The syntax of composition of workflows will remain the same, since a workflow object could be passed explicitly as an annotation argument.

```
@context(function[Env] $ option)  
def eval: Expr => Env => Option[Int] = {  
  case Var(x) => fetch(x)  
  case Val(n) => $(n)  
  case Add(x, y) => $(eval(x) + eval(y))  
}
```

**Wider subset of Scala.** The current implementation is rather conservative with respect to Scala features it supports. This is a deliberate choice, however in the future we hope to support a wider subset of Scala features, such as loops, exceptions and lazy evaluations. A possible implementation would include adding more basic workflow traits with corresponding rewriting rules, similarly to `F#`.

**Context inference.** `scala-workflow` generally reduces the amount of boilerplate code needed to support effectful computations. It can be reduced even more in the case of simple one-line expressions. For example, it could have been inferred that the expression `List(1, 2, 3) + 4` should be evaluated in the `Workflow[List]` context and avoid wrapping `$(List(1, 2, 3) + 4)` in the context declaration explicitly. However, a few problems need to be solved.

It is generally not clear which type constructor should be chosen in case it is a subtype of another type constructor. For example, the expression `Some(42)` would be expected to be evaluated in the `Workflow[Option]`, yet it has the type `Some[Int]`, which is a subtype of `Option[Int]`.

Moreover, when the type of the expression is built from a type constructor applied to more than one argument it might be ambiguous, which of them should be fixed. For example, an expression of type `Either[A, B]` can be evaluated both in the workflow of `Either[A, _]` and `Either[_ , B]`.

**Workflow inference.** As noted before, Scala's standard library does not explicitly have a `Monad` interface, but rather the expansion of `for`-expressions expects an object to have `map`, `flatMap` and `filter` methods. Hence, `scala-workflow` has to have a trivial workflow implementation for every class with a monadic interface that follows this convention, which affects extensibility of the library. An alternative approach could be to automatically infer a `SemiMonad` instance in case the `map` and `flatMap` methods are present in the class.

**Other formalisations of effects.** Despite the focus on the abstract methods of the `Workflow` trait rather than specific algebraic structures, `scala-workflow` is still heavily influenced by the famous functor/idiom/monad hierarchy of computation types. It would be interesting to see if our approach to syntactic extensions could be adapted to other formalisations of effects, particularly to comonads [26] and `codonotation` [18], and also if both formalisations can be unified in one extension.

<sup>5</sup><http://scalamacros.org/news/2014/04/21/macro-paradise-2.0.0-final.html>

## 6. CONCLUSIONS

The main contribution of this work is `scala-workflow`, a macro-based syntactic extension for Scala.

The choice of an abstract Workflow interface instead of predefined interfaces for computation types enables a uniform syntax for all computation types that can be expressed with methods available for extension. It also leaves space for further extensions, that can facilitate support of Scala features, not available with the current implementation.

The type-directed expression rewriting algorithm allows users to transparently blend effectful and pure functions in a bounded context. This offers a trade-off between an explicit structure of effects and syntactic flexibility. We argue that the latter can provide better separation of concerns, because the program maintains its logical structure, while effect handling ends up being hidden inside a workflow instance implementation.

The most similar approach was taken in F#'s computation expressions. The key distinction of `scala-workflow` is that it does not need an extended set of keywords for marking effectful computations. Moreover, it is implemented not as a compiler extension, but rather as a macro-based library, that operates with syntax trees and the type checker API.

`scala-workflow` primarily aims to enhance the syntax of effectful computations. At the same, a type constructor in the given workflow implementation is not required to semantically capture computational effects, it can simply represent a generic data structure. This makes `scala-workflow` suitable for a wide range of monadic and applicative domain-specific languages.

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