





Objects of the class Rational have two members, numer and denom.

We select the members of an object with the infix operator '.' (like in Java).

Exemple :

```
scala> val x = new Rational(1, 2)
scala> x.numer
1
scala> x.denom
2
```

Working with objects

We can now define the arithmetic functions that implement the standard rules.

3

 $\begin{array}{rcl} \frac{n_1}{d_1} + \frac{n_2}{d_2} &=& \frac{n_1 d_2 + n_2 d_1}{d_1 d_2} \\ \frac{n_1}{d_1} - \frac{n_2}{d_2} &=& \frac{n_1 d_2 - n_2 d_1}{d_1 d_2} \\ \frac{n_1}{d_1} \cdot \frac{n_2}{d_2} &=& \frac{n_1 n_2}{d_1 d_2} \\ \frac{n_1}{d_1} / \frac{n_2}{d_2} &=& \frac{n_1 d_2}{d_1 n_2} \\ \frac{n_1}{d_1} = \frac{n_2}{d_2} & \text{iff} \quad n_1 d_2 = d_1 n_2 \end{array}$

Exemple :

5

Methods

One could go further and also package functions operating on a data abstraction in the data abstraction itself.

Such functions are called methods.

Exemple : Rational numbers now would have, in addition to the functions numer and denom, the functions add, sub, mul, div, equal, toString.

One might, for example, implement this as follows:

```
class Rational(x: Int, y: Int) {
    def numer = x
    def denom = y
    def add(r: Rational) =
        new Rational(
            numer * r.denom + r.numer * denom,
            denom * r.denom)
    def sub(r: Rational) =
```



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```
class Rational(x: Int, y: Int) {
      private def gcd(a: Int, b: Int): Int = if(b == 0) a else gcd(b, a \% b)
      private val g = gcd(x, y)
       def numer = x / g
       def denom = y / g
    }
gcd and g are private members; we can only access them from inside the
Rational class.
With this definition, we obtain:
    scala> val x = new Rational(1, 3)
    scala> val y = new Rational(5, 7)
    scala> val z = new Rational(3, 2)
    scala > x.add(y).mul(z)
    11/7
In this example, we calculate gcd immediately, because we expect that the
functions numer and denom are often called.
```



Self Reference

}

On the inside of a class, the name **this** represents the object on which the current method is executed.

Exemple : Add the functions less and max to the class Rational.

```
class Rational(x: Int, y: Int) {
    //...
    def less(that: Rational) =
        numer * that.denom < that.numer * denom
    def max(that: Rational) = if (this.less(that)) that else this</pre>
```

Note that a simple name x, which refers to another member of the class, is an abbreviation of **this**.x. Thus, an equivalent way to formulate *less* is as follows.

def less(that: Rational) =
 this.numer * that.denom < that.numer * this.denom</pre>

11

Constructors The constructor introduced with the new type Rational is called the

primary constructor of the class.

Scala also allows the declaration of auxillary constructors named *this*.

Exemple : Add an auxillary constructor to the class *Rational*.

```
class Rational(x: Int, y: Int) {
    def this(x: Int) = this(x, 1)
    //...
```

```
}
```

With this definition, we obtain:

scala > val x = new Rational(2)scala > val y = new Rational(1, 2)scala > x.mul(y)1/1

Classes and Substitutions

We previously defined the meaning of a function application using a computation model based on substitution. Now we extend this model to classes and objects.

Question: How is an instantiation of the class $new C(e_1, ..., e_m)$ evaluted?

Answer: The expression arguments $e_1, ..., e_m$ are evaluated like the arguments of a normal function. That's it. The resulting expression, say, **new** $C(v_1, ..., v_m)$, is already a value.

Now suppose that we have a class definition,

class
$$C(x_1, ..., x_m) \{ ... def f(y_1, ..., y_n) = b ... \}$$

where

- The formal parameters of the class are $x_1, ..., x_m$.
- The class defines a method f with formal parameters $y_1, ..., y_n$.

13

(The list of function parameters can be absent. For simplicity, we have omitted the parameter types.)
Question: How is the expression new C(v₁, ..., v_m).f(w₁, ..., w_n) evaluated?
Answer: The expression can be rewritten as:

[w₁/y₁, ..., w_n/y_n]
[v₁/x₁, ..., v_m/x_m]
[new C(v₁, ..., v_m)/this] b

There are three substitutions at work here:

1. the substitution of the formal parameters y₁, ..., y_n of the function f by the arguments w₁, ..., w_n,
2. the substitution of the formal parameters x₁, ..., x_m of the class C by the class arguments v₁, ..., v_m,
3. the substitution of the self reference this by the value of the object new C(v₁, ..., v_n).







- A letter, followed by a sequence of letters or numbers
- An operator symbol, followed by other operator symbols.

The priority of an operator is determined by its first character.

The following table lists the characters in ascending order of priority:

(all letters) | & < > = ! : + - * / %(all other special characters) Therefore, we can define Rational more naturally:

```
class Rational(x: Int, y: Int) {
  private def gcd(a: Int, b: Int): Int = if (b == 0) a else <math>gcd(b, a \% b)
   private val g = gcd(x, y)
   def numer = x / g
   def denom = y / g
   def + (r: Rational) =
     new Rational(
        numer * r.denom + r.numer * denom,
        denom * r.denom)
   def - (r: Rational) =
     new Rational(
        numer * r.denom - r.numer * denom,
        denom * r.denom)
   def * (r: Rational) =
     new Rational(
        numer * r.numer,
        denom * r.denom)
   //...
   override def toString() = numer + "/" + denom
}
```

```
... and rational numbers can be used like Int or Double:
```

```
scala> val x = new Rational(1, 2)
scala> val y = new Rational(1, 3)
scala> x * x + y * y
13/36
```

19

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```
class NonEmpty(elem: Int, left: IntSet, right: IntSet) extends IntSet {
       def contains(x: Int): Boolean = \{
         if (x < elem) left contains x
          else if (x > elem) right contains x
          else true }
       def incl(x: Int): IntSet = {
         if (x < elem) new NonEmpty(elem, left incl x, right)
         else if (x > elem) new NonEmpty(elem, left, right incl x)
         else this }
    }
Remarks:
  • Empty and NonEmpty both extend the class IntSet.
  • This means that the types Empty and NonEmpty conform to the type
    IntSet: an object of type Empty or NonEmpty can be used wherever
    an object of type IntSet is required.
                                     22
```







Exemp	le :
	(new NonEmpty(7, new Empty, new Empty)).contains(1)
\rightarrow	
	$\mathbf{if} (1 < 7) \mathbf{new} \text{ Empty contains } 1$
	else if $(1 > 7)$ new Empty contains 1
	else true
\rightarrow	
	new Empty contains 1
\rightarrow	falso
Dynami	c dispatch of methods is analogous to calls to higher-order
function	S.
• • •	
Questio	1:
Can we	implement one concept in terms of the other?

Standard Classes

In fact, types such as *Int* or *Boolean* do not receive special treatment in Scala. They are like the other classes, defined in the package *scala*.

For reasons of efficiency, the compiler usually represents the values of type scala.Int by 32-bit integers, and the values of type scala.Boolean by Java's Booleans, etc.

But this is just an optimization, this doesn't have any effect on the meaning of a program.

Here is a possible implementation of the class Boolean.

The class Boolean package scala trait Boolean { **def** if ThenElse[a]($t: \Rightarrow a$)($e: \Rightarrow a$): a $def \&\& (x: \Rightarrow Boolean): Boolean = ifThenElse[Boolean](x)(false)$ $def \mid \mid (x: \Rightarrow Boolean): Boolean = ifThenElse[Boolean](true)(x)$ def ! : Boolean = ifThenElse[Boolean](false)(true) def == (x: Boolean): Boolean = ifThenElse[Boolean](x)(x.!)def := (x: Boolean): Boolean = ifThenElse[Boolean](x.!)(x)def < (x: Boolean): Boolean = ifThenElse[Boolean](false)(x)def > (x: Boolean): Boolean = ifThenElse[Boolean](x.!)(false) $def \leq (x: Boolean): Boolean = ifThenElse[Boolean](x)(true)$ def > (x: Boolean): Boolean = ifThenElse[Boolean](true)(x.!)} val true = new Boolean { def if ThenElse[a]($t: \Rightarrow a$)($e: \Rightarrow a$) = t } val false = new Boolean { def if ThenElse[a]($t: \Rightarrow a$)($e: \Rightarrow a$) = e }





Pure Object OrientationA pure object-oriented language is one in which each value is an object.If the language is based on classes, this means that the type of each value is a class.Is Scala a pure object-oriented language?We have seen that Scala's numeric types and the Boolean type can be implemented like normal classes.We'll see next week that functions can also be seen as objects.The function type $A \Rightarrow B$ is treated like an abbreviation for objects that have a method for application:def apply(x: A): B

31

<section-header><section-header><list-item><list-item><list-item><list-item><list-item><list-item>

Language Elements Introduced This Week

Types:

 $Type = ... \mid ident$

A type can now be an identifier, i.e., a class name.

Expressions:

 $Expr = \dots | new Expr | Expr '.' ident$

An expression can now be an object creation or a selection E.m of a member m of an expression E whose value is an object

Def	$= FunDef \mid ValDef \mid ClassDef$
ClassDef	= [abstract] class ident ['(' [Parameters] ')']
TemplateDef	= [Modifier] Def
Modifier	= AccessModifier override
AccessModifie	${f r} = {f private} \ \ {f protected}$
A definition can :	now be a class definition such as
class C(paran	ms) extends $B \{ defs \}$
Definitions defs is	n a class can be preceeded by modifiers private ,
protected or ov	rerride.