Type Systems

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Slides in part adapted from: University of Pennsylvania CIS 500: Software Foundations - Fall 2006 by Benjamin Pierce

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The main part of this course is about type systems

But in a larger sense the course is about software foundations

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What is "software foundations"?

Software foundations (or "theory of programming languages") is the mathematical study of the meaning of programs.

The goal is finding ways to describe program behaviors that are both precise and abstract.

- precise so that we can use mathematical tools to formalize and check interesting properties
- abstract so that properties of interest can be discussed clearly, without getting bogged down in low-level details





What this course is not

- An introduction to programming
- A course on functional programming (though we'll be doing some functional programming along the way)
- A course on compilers (you should already have basic concepts such as lexical analysis, parsing, abstract syntax, and scope under your belt)
- A comparative survey of many different programming languages and styles

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Approaches to Program Meaning

- Denotational semantics and domain theory view programs as simple mathematical objects, abstracting away their flow of control and concentrating on their input-output behavior.
- Program logics such as Hoare logic and dependent type theories focus on logical rules for reasoning about programs.
- Operational semantics describes program behaviors by means of abstract machines. This approach is somewhat lower-level than the others, but is extremely flexible.
- Process calculi focus on the communication and synchronization behaviors of complex concurrent systems.
- Type systems describe approximations of program behaviors, concentrating on the shapes of the values passed between different parts of the program.

Overview

In this course, we will concentrate on operational techniques and type systems.

- ► Part I: Modeling programming languages
 - ▷ Syntax and parsing
 - Operational semantics
 - Inductive proof techniques
 - ▷ The lambda-calculus
 - Syntactic sugar; fully abstract translations
- ► Part II: Type systems
 - ▷ Simple types
 - ▶ Type safety
 - References
 - Subtyping

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Overview

- ▶ Part III: Object-oriented features (case study)
 - > A simple imperative object model
 - ▷ An analysis of core Java
 - An analysis of core Scala

Organization of the Course

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People	
Instructor:	Martin Odersky
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Information

Textbook:	Types and Programming Languages,
	Benjamin C. Pierce, MIT Press, 2002

Webpage: http://lampwww.epfl.ch/teaching/typeSystems/

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Homework and Projects

You will be asked to

- solve and hand in some written exercise sheets,
- do a number of programming assignments, including
 - ▶ parsers,
 - ▷ interpreters and reduction engines,
 - ▶ type checkers

for a variety of small languages.

The recommended implementation language for these assignments is Scala.

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Grading and Exams

Final course grades will be computed as follows:

- ▶ Homework and project: 30%
- ▶ Mid-term exam: 30% each
- ► Final exam: 40%

Exams:

- 1. Mid-term: Wed, Dec 20th, 2006
- 2. Final exam: Wed, Feb 7th, 2007

(dates are provisional)



Part I

Modelling programming languages









A Hosted Grammar Description Language in Scala

We will develop a framework where grammars can be described like this:

```
\begin{array}{lll} \mathsf{def} \ \mathsf{Expr} & : \mathsf{Parser} = \mathsf{Term} \ \& \ \mathsf{rep}(\mathsf{kw}("+") \ \& \ \mathsf{Term} \ | \ \mathsf{kw}("-") \ \& \ \mathsf{Term}) \\ \mathsf{def} \ \mathsf{Term} & : \mathsf{Parser} = \mathsf{Factor} \ \& \ \mathsf{rep}(\mathsf{kw}("*") \ \& \ \mathsf{Factor} \ | \ \mathsf{kw}("/") \ \& \ \mathsf{Factor}) \\ \mathsf{def} \ \mathsf{Factor} : \ \mathsf{Parser} = \mathsf{numericLit} \ | \ \mathsf{kw}("(") \ \& \ \mathsf{Expr} \ \& \ \mathsf{kw}(")") \end{array}
```

This description can be produced from the previous grammar by systematic text replacements:

- Insert a def at the beginning of each production.
- ► The "::=" becomes ": Parser =".
- Sequential composition is now expressed by a &.
- ▶ Repetition {...} is now expressed by rep(...).
- ▶ Option [...] is now expressed by opt(...).

Terminal symbols appear inside kw(...).
The point at the end of a production is removed.

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The Basic Idea in Code

```
class GenericParsers {
type Parser = Input \Rightarrow ParseResult
```

where

```
type Input = List[Token] or type Input = Stream[Token]
```

and we assume:

- ► A class Token with subclasses
 - ▷ case class KW(chars: String) for keywords,
 - case class NumericLit(chars: String) for numbers,
 - case class StringLit(chars: String) for strings,
 - ▷ case class Identifier(chars : String) for identifiers.

In each case, chars represents the characters making up the token.

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The opt(P) combinator is equivalent to P if P succeeds and is equivalent to empty if P fails.

• The rep(P) combinator applies P zero or more times until P fails.

The two combinators are implemented as follows:

def opt(p: Parser): Parser = p | emptydef rep(p: Parser): Parser = p & rep(p) | empty

Note that neither of these combinators can fail!

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Other Combinators

More combinators can be defined if necessary.

Exercise: Implement the rep1(P) parser combinator, which applies P one or more times.

Exercise: Define opt and rep directly, without making use of &, |, and empty.





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```



We now design a program that

...

- accepts as input an arithmetic expression (given as a string)
- > yields as output the result of evaluating the expression,
- > or produces an error message if the expression is not well-formed.

The program uses the combinator parsing library:

```
object ExprParser extends TokenizingParsers // it parses from array of characters
with BuildingParsers // it constructs some result
with Application { // it has a main method
```





Arithmetic expression grammar

```
► The rest of the grammar is as before:
def Expr : Parser = production (
Term & rep(kw("+") & Term | kw("-") & Term)
)
def Term : Parser = production (
Factor & rep(kw("*") & Factor | kw("/") & Factor)
)
def Factor : Parser = production (
numericLit
| kw("(") & Expr & kw(")")
| failure("illegal start of expression")
)
```

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```

Computing Results ► To compute expression results, we first have to fix the Output type and the build function: type Output = int def build(xs: List[Token], pos: Position) = eval(xs) > We then have to write an evaluation function, which takes a list of tokens and yields an integer result. def eval(xs: List[Token]): Output = xs match { case NonTerminal(t1) :: KW("+") :: NonTerminal(t2) :: rest \Rightarrow eval(NonTerminal(t1 + t2) :: rest)// analogous for -, *, and / case List(NumericLit(n)) \Rightarrow Integer.parseInt(n) case List(KW("("), t, KW(")")) \Rightarrow t case List(NonTerminal(result)) \Rightarrow result }



