

Transactional Memories: a theoretical introduction



Selim Arsever & Pascal Perez

Shared Memory Problems

$$M(w,r,v) := w(f).M < w, r, f > + \underline{r} < v >.M < w, r, v >$$

$$A(w,r) := \underline{w} < v >.WORK.r(v').[v' = v].A$$

$$\underline{A} < w, r > \mid \underline{A} < w, r > \mid M < w, r, v > =$$

$$\underline{w} < v >.WORK.r(v').[v' = v].A \mid$$

$$\underline{w} < v >.WORK.r(v').[v' = v].A \mid$$

$$w(f).M < w, r, f > + \underline{r} < v >.M < w, r, v >$$

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→

$$\underline{w} < a >.WORK.r(v').[v' = a].A \mid$$

$$\underline{w} < v >.WORK.r(v').[v' = v].A \mid$$

$$w(a).M < w, r, f > + \underline{r} < v >.M < w, r, v >$$

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$$w(f).M < w, r, f > + \underline{r} < a >.M < w, r, a >$$

Shared Memory Problems

$$M(w,r,v) := w(f).M<w,r,f> + \underline{r}<v>.M<w,r,v>$$

$$A(w,r) := \underline{w}<v>.WORK.r(v').[v'=v].A$$

→

$$\underline{w}<a>.WORK.r(v').[v'=a].A \mid$$

$$\underline{\textcolor{red}{w}}<\textcolor{red}{b}>.WORK.r(v').[v'=b].A \mid$$

$$\textcolor{red}{w(b)}.M<w,r,b> + \underline{r}<a>.M<w,r,a>$$

Shared Memory Problems

$$M(w,r,v) := w(f).M<w,r,f> + \underline{r}<v>.M<w,r,v>$$

$$A(w,r) := \underline{w}<v>.WORK.r(v').[v'=v].A$$

→

$$\underline{w}<a>.WORK.r(v').[v'=a].A \mid$$

$$\underline{w}.WORK.r(v').[v'=b].A \mid$$

$$w(b).M<w,r,b> + \underline{r}<a>.M<w,r,a>$$

Shared Memory Problems

$$M(w,r,v) := w(f).M < w, r, f > + \underline{r} < v >.M < w, r, v >$$

$$A(w,r) := \underline{w} < v >.WORK.r(v').[v' = v].A$$

→

$$\underline{w} < a >.WORK.r(v').[v' = a].A \mid$$

$$\underline{w} < b >.WORK.r(v').[v' = b].A \mid$$

$$w(f).M < w, r, f > + \underline{r} < b >.M < w, r, b >$$

Shared Memory Problems

$$M(w,r,v) := w(f).M < w, r, f > + \underline{r} < v >.M < w, r, v >$$

$$A(w,r) := \underline{w} < v >.WORK.r(v').[v' = v].A$$

→

$$\underline{w} < a >.WORK.r(v').[\textcolor{red}{b} = a].A \mid$$

$$\underline{w} < b >.WORK.r(v').[v' = b].A \mid$$

$$w(f).M < w, r, f > + \textcolor{red}{r} < b >.M < w, r, b >$$

Shared Memory Problems

$$M(w,r,v) := w(f).M < w, r, f > + \underline{r} < v >.M < w, r, v >$$

$$A(w,r) := \underline{w} < v >.WORK.r(v').[v' = v].A$$

→

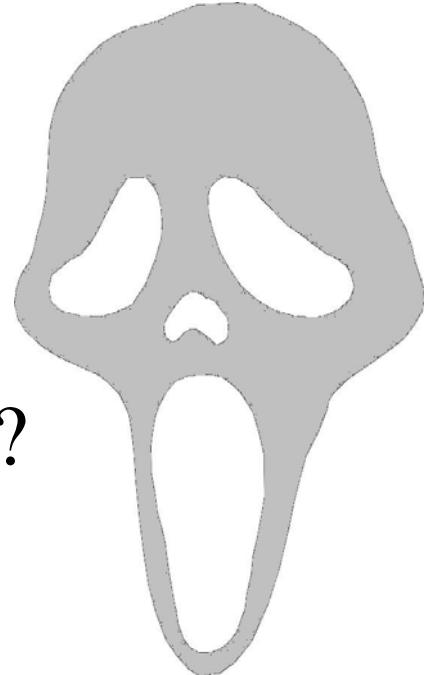
$$\underline{w} < a >.WORK.r(v').[\textcolor{red}{b} = a].A \mid$$

$$\underline{w} < b >.WORK.r(v').[v' = b].A \mid$$

$$w(f).M < w, r, f > + \underline{r} < b >.M < w, r, b >$$

Locking is dangerous

- What if a thread fails whilst holding a lock?
- Deadlocks happen!
- Linux pros on <http://lwn.net/Articles/86859/>



Locking does not scale well

Fine grained locked data structures implementation
exist of the shelf but...

Global knowlegde!



Transaction

Atomicity

Consistency

Isolation

Durability

Transaction

$A + B + C$ should remain constant under the execution of both transactions in any order.

Correct:

$A = A - 10$
 $lock L_1$
 $B = B + 10$
 $unlock L_1$

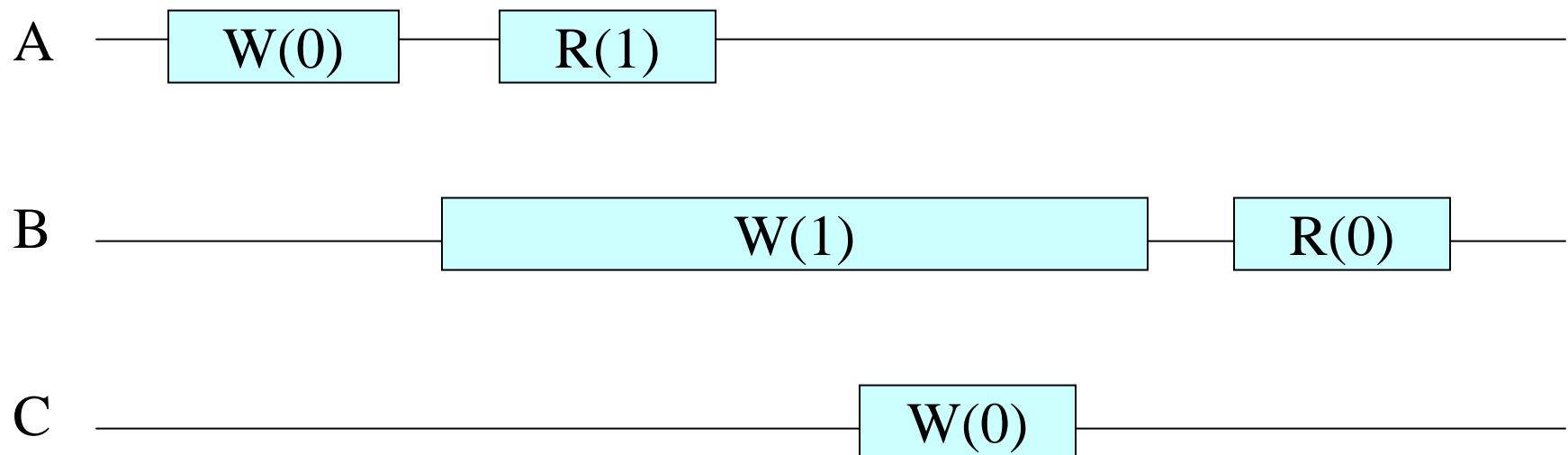
$lock L_1$
 $B = B - 20$
 $unlock L_1$
 $C = C + 20$

Wrong:

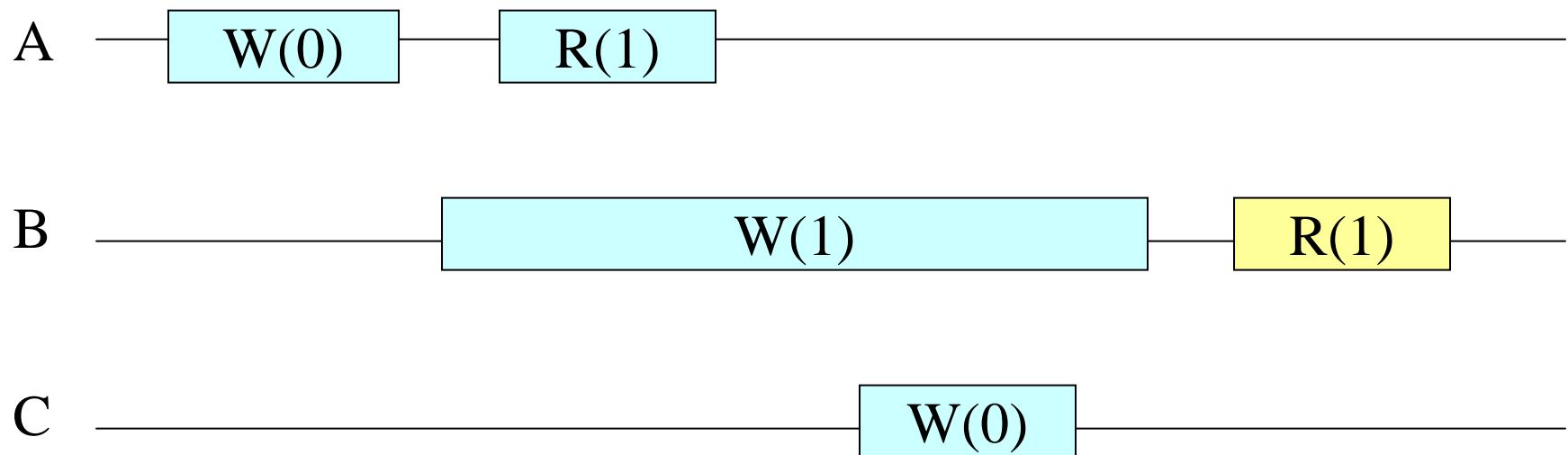
$lock L_1$
 $A = A - 10$
 $unlock L_1$
 $B = B + 10$

$lock L_2$
 $B = B - 20$
 $unlock L_2$
 $C = C + 20$

Transactional Memory

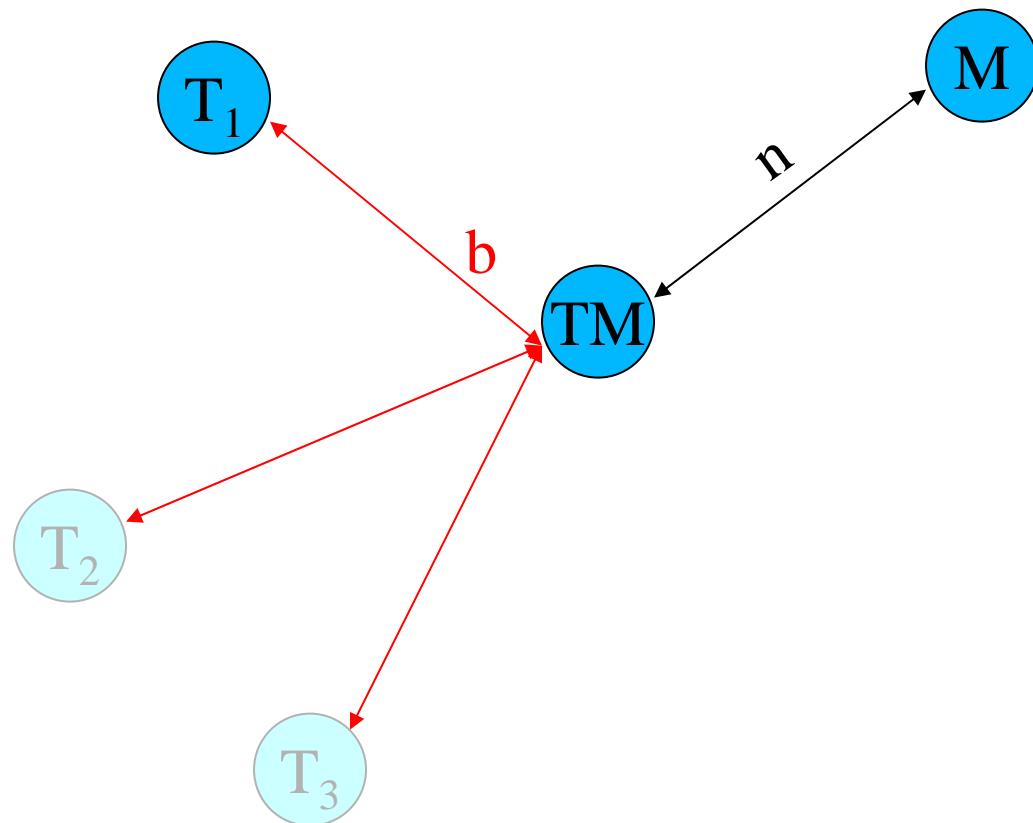


Transactional Memory



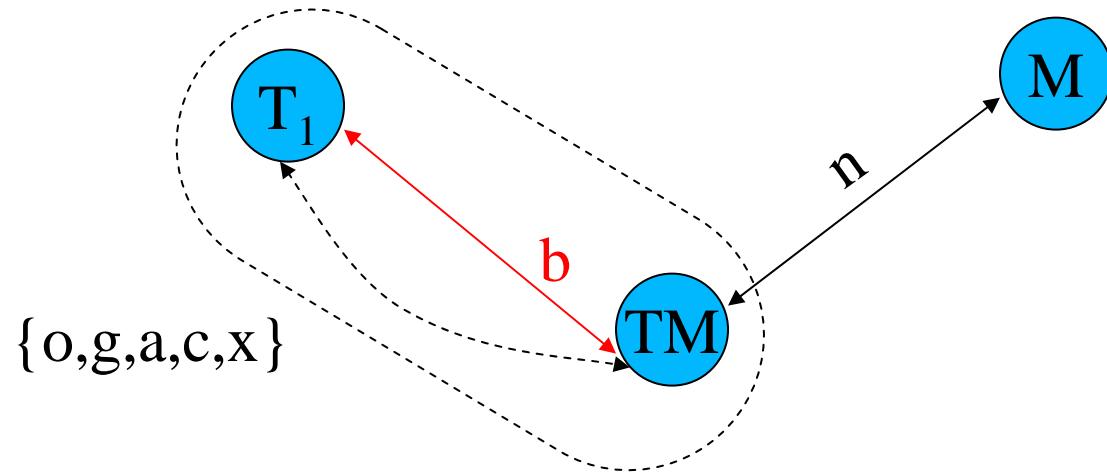
Transactional Memory

Initial Situation:



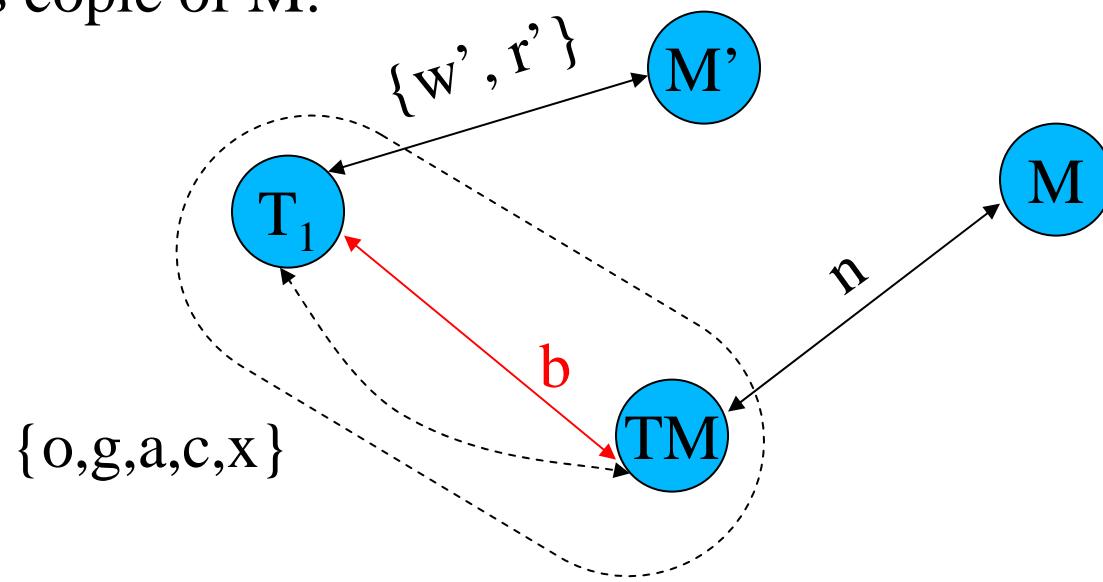
Transactional Memory

T_1 gives his channels to TM:



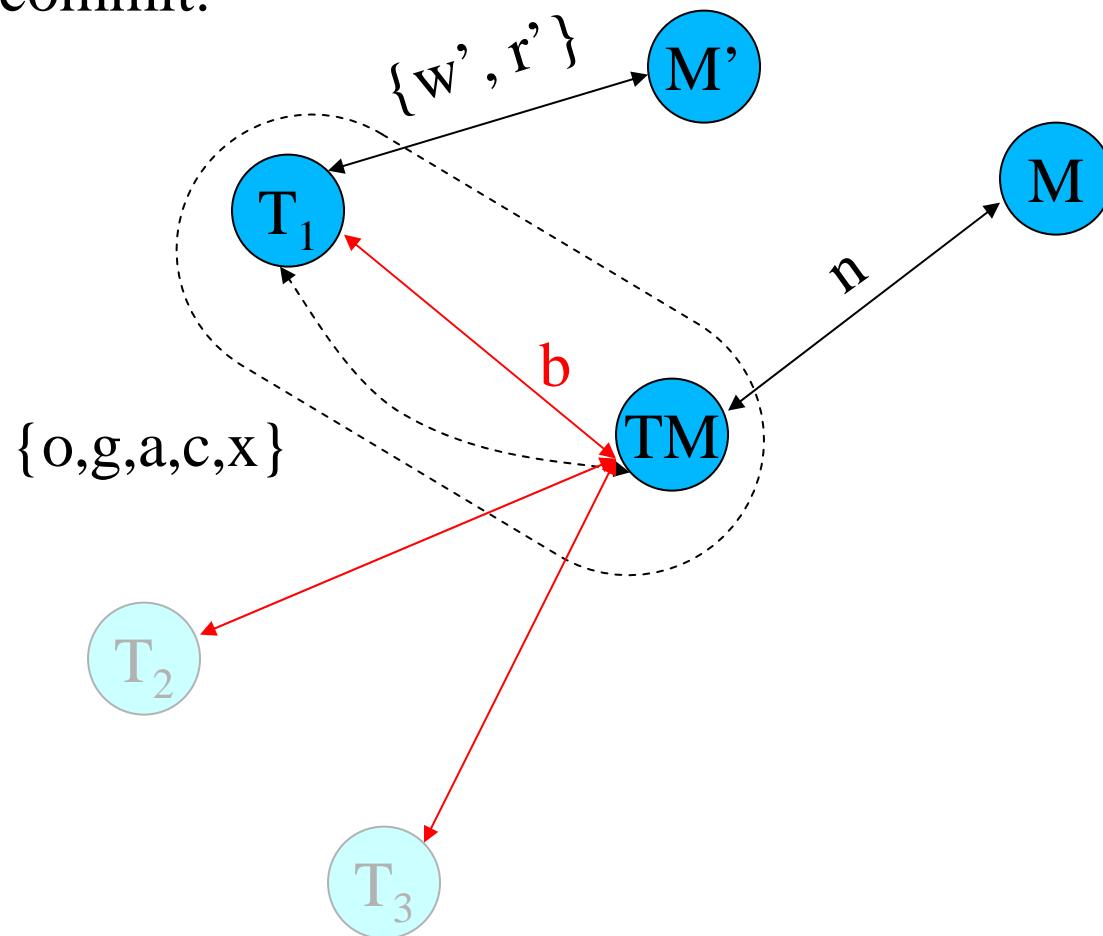
Transactional Memory

T_1 gets it's copie of M :



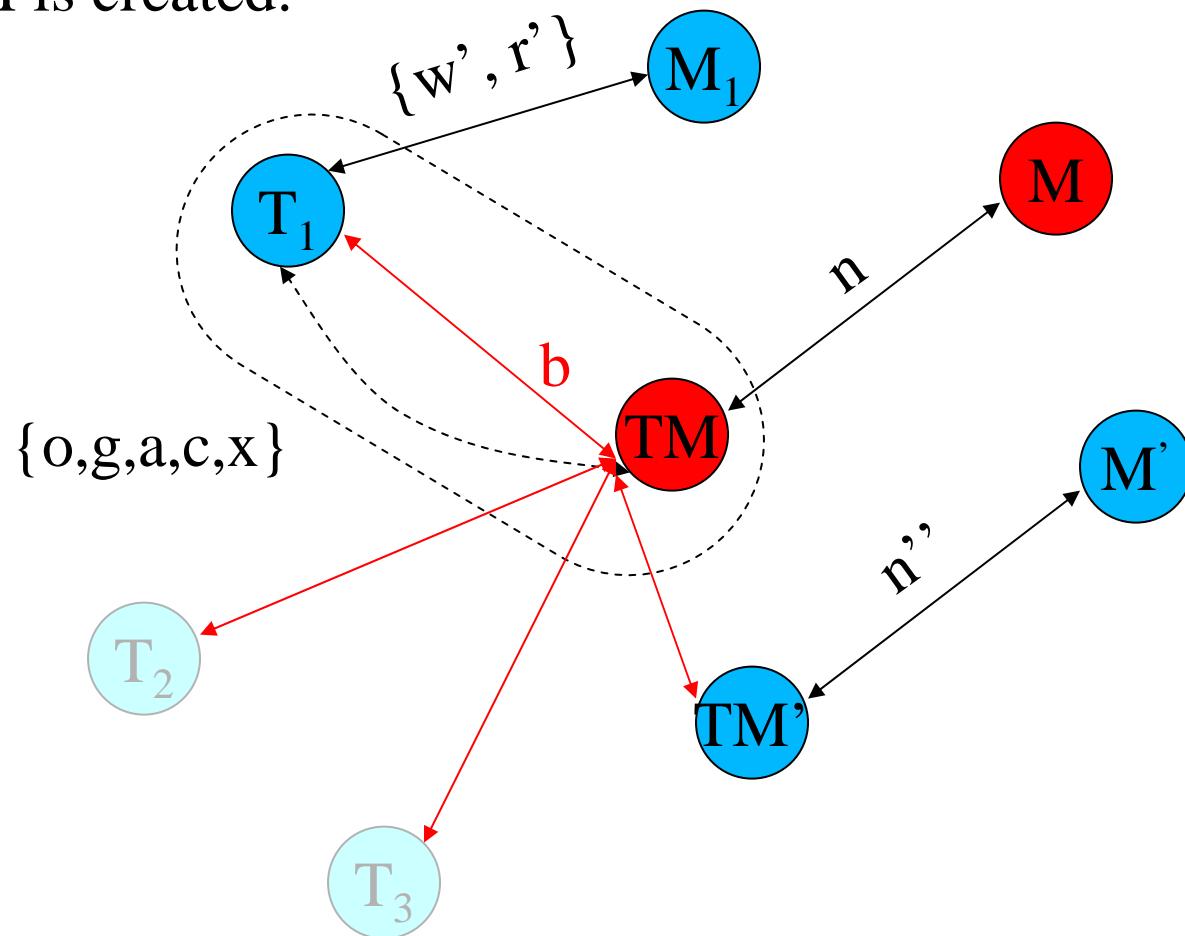
Transactional Memory

T_1 tries to commit:



Transactional Memory

A new TM is created:



Concurrent Commit

$T_1 : \underline{c}_1.(c_1 + x_1.T_1 < b >)$

$T_2 : \underline{c}_2.(c_2 + x_2.T_2 < b >)$

$TM : \underline{\text{crash}} \mid !\dots \mid k.\underline{x}_1 \mid k.\underline{x}_2 \mid ! p(x).k.\underline{x} \mid$

$c_1.\text{crash}.n_1''(w'', r'', n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_1) \mid$

$c_2.\text{crash}.n_2''(w'', r'', n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_2)$

Concurrent Commit

$T_1 : \underline{c}_1.(c_1 + x_1.T_1 < b >)$

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$\underline{c}_1.\text{crash}.n_1'(w'', r'', n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_1) \mid$

$\underline{c}_2.\text{crash}.n_2'(w'', r'', n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_2) \mid$

Concurrent Commit

$T_1 : \underline{c}_1.(c_1 + x_1.T_1)$

$T_2 : \underline{c}_2.(c_2 + x_2.T_2)$

$TM : \underline{\text{crash}} \mid !\dots \mid k.\underline{x}_1 \mid k.\underline{x}_2 \mid ! p(x).k.\underline{x} \mid$

$c_1.\underline{\text{crash}}.n_1''(w'', r'', n'').(TM <b, n''> \mid !\underline{k} \mid \underline{c}_1) \mid$

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$c_1.\underline{\text{crash}}.n_1''(w'', r'', n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_1) \mid$

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Concurrent Commit

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 $c_2.\underline{\text{crash}}.n_2''(w'',r'',n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_2)$

Concurrent Commit

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 $c_2.\underline{\text{crash}}.n_2''(w'', r'', n'').(TM < b, n'' > \mid !\underline{k} \mid \underline{c}_2)$

Exceptions Enhancement

- Avoiding Unnecessary Exceptions

$$TM := (\dots \mid !p(x, \text{cancel}).(k.x + \text{cancel}))$$
$$G := \dots (v\text{cancel})(p<x, \text{cancel}>. \dots .(\dots \mid \text{cancel}.!k))$$

- Allowing Needed Exceptions

Commit while Starting

$T_1 : \underline{c}_1.(c_1 + x_1.T_1)$

$T_2 : b <o_2, g_2, a_2, c_2, x_2 >. \underline{o}. g \dots$

$TM : \underline{\text{crash}} \mid !\dots \mid k.\underline{x}_1 \mid ! p(x).k.\underline{x} \mid$

$c_1.\text{crash}.n_1''(w'', r'', n'').(TM <b, n''> \mid !\underline{k} \mid \underline{c}_1) \mid$

$b(o_2, g_2, a_2, c_2, x_2).p <x_2>. \underline{o} \dots$

Commit while Starting

$T_1 : \underline{c}_1.(c_1 + x_1.T_1)$

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Commit while Starting

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$b(o_2, g_2, a_2, c_2, x_2). \underline{p} < x_2 >. \underline{o} \dots$

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$TM : \underline{\text{crash}} \mid !\dots \mid k.\underline{x}_1 \mid ! p(x).k.\underline{x} \mid$

$c_1.\text{crash}.n_1' (w'', r'', n'').(TM < b, n'' >) \mid !\underline{k} \mid \underline{c}_1 \mid$

$b(o_2, g_2, a_2, c_2, x_2).p < x_2 >. \underline{O} \dots$

Commit while Starting

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$T_2 : b < o_2, g_2, a_2, c_2, x_2 >. \underline{O}.g \dots$

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 $c_1.\text{crash}.n_1''(w'', r'', n'').(TM < b, n' > \mid !\underline{k} \mid \underline{c}_1) \mid$
 $b(o_2, g_2, a_2, c_2, x_2).p < x_2 >. \underline{O} \dots$

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 $c_1.\text{crash}.n_1''(w'', r'', n'').(TM <b, n''> \mid !\underline{k} \mid \underline{c}_1) \mid$
 $b(o_2, g_2, a_2, c_2, x_2).p <x_2>. \underline{o} \dots$