

# Transactional Memories: a theoretical introduction



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## Shared Memory Problems

$$M(w,r,v) := w(f).M\langle w,r,f \rangle + \underline{r}\langle v \rangle.M\langle w,r,v \rangle$$

$$A(w,r) := \underline{w}\langle v \rangle.WORK.r(v').[v'=v].A$$

→

$$\underline{w}\langle a \rangle.WORK.r(v').[v'=a].A \mid$$

$$\underline{w}\langle v \rangle.WORK.r(v').[v'=v].A \mid$$

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$$\underline{A}\langle w,r \rangle \mid \underline{A}\langle w,r \rangle \mid M\langle w,r,v \rangle =$$

$$\underline{w}\langle v \rangle.WORK.r(v').[v'=v].A \mid$$

$$\underline{w}\langle v \rangle.WORK.r(v').[v'=v].A \mid$$

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$$\underline{w}\langle a \rangle.WORK.r(v').[v'=a].A \mid$$

$$\underline{w}\langle b \rangle.WORK.r(v').[v'=b].A \mid$$

$$w(b).M\langle w,r,b \rangle + \underline{r}\langle a \rangle.M\langle w,r,a \rangle$$

## Shared Memory Problems

$$M(w,r,v) := w(f).M\langle w,r,f \rangle + \underline{r}\langle v \rangle.M\langle w,r,v \rangle$$

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$$\underline{w}\langle a\rangle.WORK.r(v').[v'=a].A \mid$$
$$\underline{w}\langle b\rangle.WORK.r(v').[v'=b].A \mid$$
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$$\underline{w}\langle a\rangle.WORK.r(v').[b=a].A \mid$$
$$\underline{w}\langle b\rangle.WORK.r(v').[v'=b].A \mid$$
$$w(f).M\langle w,r,f\rangle + \underline{r}\langle b\rangle.M\langle w,r,b\rangle$$

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$$\underline{w}\langle b\rangle.WORK.r(v').[v'=b].A \mid$$
$$w(f).M\langle w,r,f\rangle + \underline{r}\langle b\rangle.M\langle w,r,b\rangle$$

## Locking is dangerous

- What if a thread fails whilst holding a lock?
- Deadlocks happen!
- Linux pros on <http://lwn.net/Articles/86859/>



# Locking does not scale well

Fine grained locked data structures implementation exist of the shelf but...

Global knowlegde!



# Transaction

- Atomicity
- Consistency
- Isolation
- Durability

# Transaction

A + B + C should remain constant under the execution of both transactions in any order.

Correct:

```

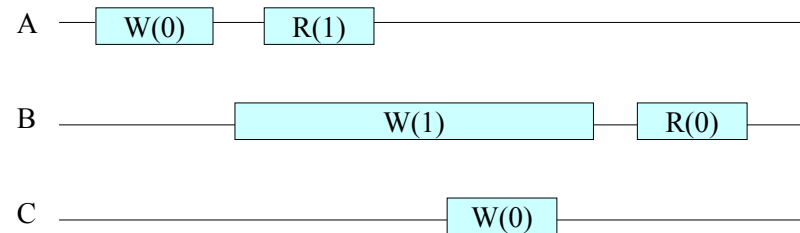
A = A - 10
lock L1
B = B - 20
unlock L1
C = C + 20
    
```

Wrong:

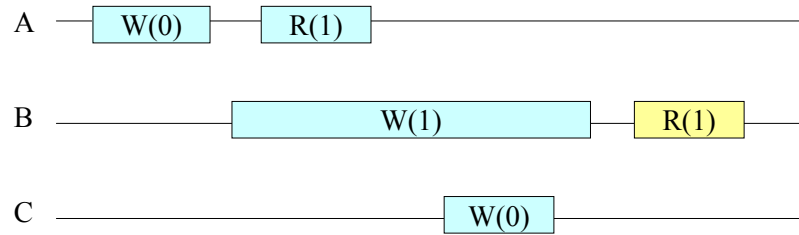
```

lock L1
A = A - 10
unlock L1
B = B + 10
lock L2
B = B - 20
unlock L2
C = C + 20
    
```

# Transactional Memory

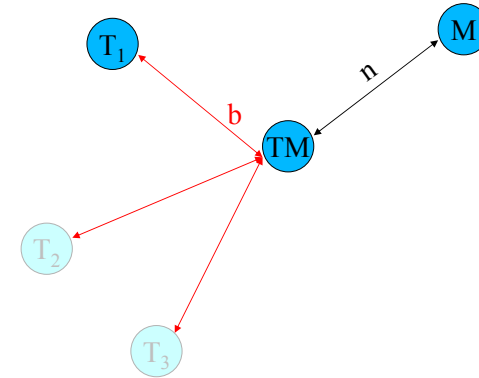


# Transactional Memory



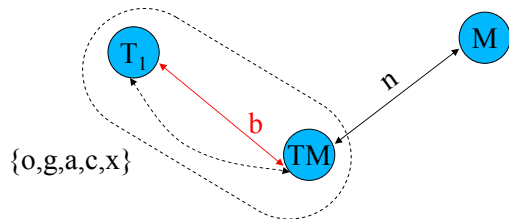
# Transactional Memory

Initial Situation:



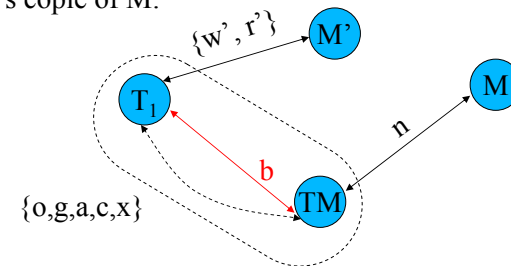
# Transactional Memory

T<sub>1</sub> gives his channels to TM:



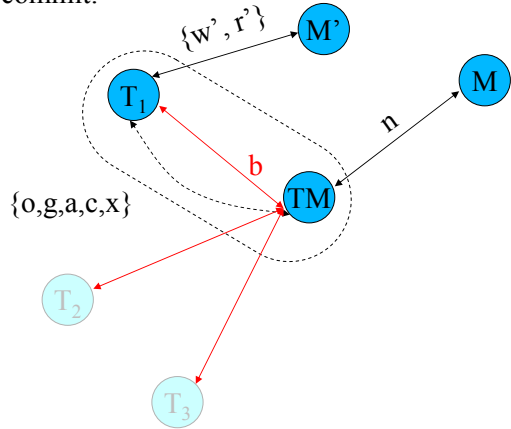
# Transactional Memory

T<sub>1</sub> gets it's copie of M:



## Transactional Memory

$T_1$  tries to commit:



## Concurrent Commit

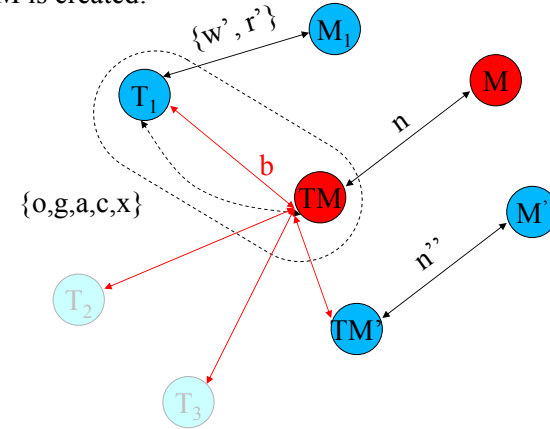
$$T_1: \underline{c}_1.(c_1 + x_1.T_1\langle b \rangle)$$

$$T_2: \underline{c}_2.(c_2 + x_2.T_2\langle b \rangle)$$

$$\begin{aligned} TM: & \underline{crash} \mid !\dots \mid k.\underline{x}_1 \mid k.\underline{x}_2 \mid ! p(x).k.\underline{x} \mid \\ & \underline{c}_1.\underline{crash}.n_1'(w'', r'', n'').(TM\langle b, n'' \rangle \mid !\underline{k} \mid \underline{c}_1) \mid \\ & \underline{c}_2.\underline{crash}.n_2'(w'', r'', n'').(TM\langle b, n'' \rangle \mid !\underline{k} \mid \underline{c}_2) \end{aligned}$$

## Transactional Memory

A new TM is created:



## Concurrent Commit

$$T_1: \underline{c}_1.(c_1 + x_1.T_1\langle b \rangle)$$

$$T_2: \underline{c}_2.(c_2 + x_2.T_2\langle b \rangle)$$

$$\begin{aligned} TM: & \underline{crash} \mid !\dots \mid k.\underline{x}_1 \mid k.\underline{x}_2 \mid ! p(x).k.\underline{x} \mid \\ & \underline{c}_1.\underline{crash}.n_1'(w'', r'', n'').(TM\langle b, n'' \rangle \mid !\underline{k} \mid \underline{c}_1) \mid \\ & \underline{c}_2.\underline{crash}.n_2'(w'', r'', n'').(TM\langle b, n'' \rangle \mid !\underline{k} \mid \underline{c}_2) \end{aligned}$$

## Concurrent Commit

$T_1: \underline{c}_1.(c_1 + x_1.T_1\langle b \rangle)$

$T_2: \underline{c}_2.(c_2 + x_2.T_2\langle b \rangle)$

TM : crash | !... | k.x<sub>1</sub> | k.x<sub>2</sub> | ! p(x).k.x |

$c_1.\text{crash}.n_1'(w'', r'', n'').(TM\langle b, n'' \rangle | !\underline{k} | \underline{c}_1) |$

$c_2.\text{crash}.n_2'(w'', r'', n'').(TM\langle b, n'' \rangle | !\underline{k} | \underline{c}_2)$

## Concurrent Commit

$T_1: \underline{c}_1.(c_1 + x_1.T_1\langle b \rangle)$

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## Concurrent Commit

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$c_2.\text{crash}.n_2'(w'', r'', n'').(TM\langle b, n'' \rangle | **!\underline{k}** | \underline{c}_2)$

## Concurrent Commit

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 $c_1.\text{crash}.n_1'(w'', r'', n'').(TM\langle b, n'' \rangle | !\underline{k} | \underline{c}_1) |$   
 $c_2.\text{crash}.n_2'(w'', r'', n'').(TM\langle b, n'' \rangle | !\underline{k} | \underline{c}_2)$

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## Exceptions Enhancement

- Avoiding Unnecessary Exceptions

TM := (... | !p(x, cancel).(k.x + cancel))

G := ... (vcancel)(p<x, cancel>. ... .(... | cancel.!k)

- Allowing Needed Exceptions

## Commit while Starting

$T_1: \underline{c}_1.(c_1 + x_1.T_1\langle b \rangle)$

$T_2: \underline{b}\langle o_2, g_2, a_2, c_2, x_2 \rangle . \underline{o}.g \dots$

TM : crash | !... | k.x<sub>1</sub> | ! p(x).k.x |  
 $c_1.\text{crash}.n_1'(w'', r'', n'').(TM\langle b, n'' \rangle | !\underline{k} | \underline{c}_1) |$   
 $\underline{b}\langle o_2, g_2, a_2, c_2, x_2 \rangle . p\langle x_2 \rangle . \underline{o} \dots$



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