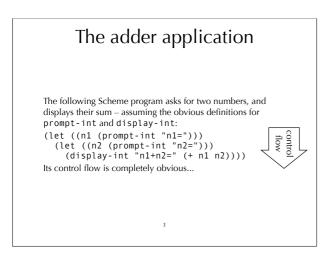
Continuations

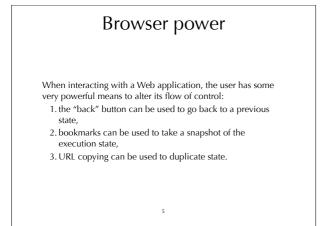
Michel Schinz Advanced Compiler Construction – 2009-03-27

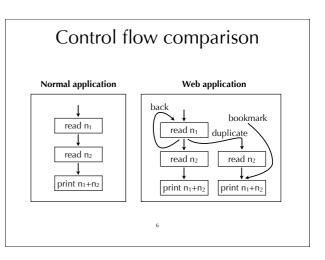
Control flow of Web applications



The adder Web application

Let's assume that we want to take our adder application and turn it into a Web application, with the requirement that every interaction happens on a separate page. That is, we want to use a first Web page to ask for the first number, a second page to ask for the second number, and a third one to display their sum. If we suppose that we have the proper primitives at our disposal, this should be trivial: (let ((n1 (web-prompt-int "n1="))) (let ((n2 (web-prompt-int "n2="))) (web-display-int "n1+n2=" (+ n1 n2)))) What about control flow?





Solutions for Web applications

Several solutions have been developed to deal with the unusual control flow of Web programs:

- 1. do nothing and let the programmer deal with the complexity e.g. PHP,
- 2. tame the browser by disabling both the "back" button and cloning e.g. JWIG,
- 3. use *continuations* to please the user and the programmer e.g. Seaside.

Suspended computations

In our adder application, each time some data has to be obtained from the user, the execution of the program is suspended. It is then resumed as soon as the user submits the data.

The power of the Web version of our application comes from the fact that those suspended computations are given a name: the URL associated with them! The user can therefore manipulate those suspended computations at will. She can for example resume the same suspended computation several times, something that is not possible with the non-Web version of the application.

Continuations

Continuations

A **continuation** is a data structure representing a suspended computation.

The main operation that can be performed on a continuation is **resuming** – or **throwing** – it. When a continuation k is resumed, the current execution of the program is replaced by the execution of k's computation.

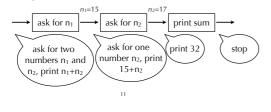
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A continuation describes how to continue a suspended computation, hence the name.

Current continuation At any given point during the execution of a program, it is

possible to talk about the **current continuation**. This continuation describes what still needs to be done in order to complete the running program.

For example, imagine that our adder application is used to sum 15 and 17. How can the current continuation be described at various points of the execution?



Continuations and the Web

In a Web application, execution is suspended each time a page is presented to the user. When the user proceeds – by clicking on a link or by submitting a form – execution is resumed. In terms of continuations, this means that the current continuation is saved on the server whenever a page is displayed, and associated with a (unique) URL. That saved continuation is resumed later when the user requests its URL.

Functions and continuations

In any programming language, when a function f calls a function g, the execution of f is suspended while g is running, and resumed as soon as g is finished.

In terms of continuations, calling a function therefore consists in saving the current continuation, and then proceed with the execution of the called function. Returning from a function consists in restoring the most recently saved continuation. In most languages, continuations can only be manipulated in that indirect fashion, through function calls and returns. However, some languages like Scheme offer first-class continuations, that is the ability to manipulate continuations like all other values.

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Continuations in Scheme

Exposing continuations

How should (first-class) continuations be exposed to the programmer?

In an object-oriented language, continuations could be represented as a class, with methods to obtain the current continuation, or resume an existing continuation.

In a functional language, continuations can be represented as *functions*. Invoking such "continuation functions" resumes the associated continuation. This is how Scheme and several other languages expose continuations.

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Continuations in Scheme

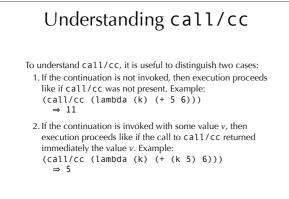
Scheme provides the primitive call-with-currentcontinuation – often abbreviated to call/cc – to obtain the current continuation.

This primitive expects a function as argument, and calls that function with the current continuation as argument, reified as a standard Scheme function.

If that function is invoked later, its continuation will be resumed, and replace the current continuation of the program. Example:

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(call/cc (lambda (k) (k 10) 20)) \Rightarrow 10



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Examples

```
\begin{array}{l} (\text{call/cc (lambda (k) 10)}) \\ \Rightarrow 10 \\ (\text{call/cc (lambda (k) (k 10))}) \\ \Rightarrow 10 \\ (+ 1 (\text{call/cc (lambda (k) (k (k 10) 20))}) \\ \Rightarrow 11 \\ (\text{call/cc (lambda (k) (k (k (k 20))))}) \\ \Rightarrow 20 \\ (\text{call/cc (lambda (k1)} \\ (+ (\text{call/cc (lambda (k2) 5)}) \\ (\text{k1 6)})) \\ \Rightarrow 6 \end{array}
```

Example use: local return Continuations can be used to return immediately from a function, like the return statement in Java. This is achieved by obtaining the current continuation at the beginning of the function, and invoking it to return. (define contains-negative? (lambda (l) (call/cc (lambda (return) (for-each (lambda (e) (if (< e 0)

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1)

#f))))

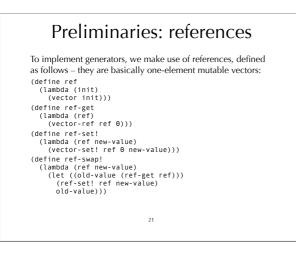
false in Scheme

(return #t)))

true in Scheme

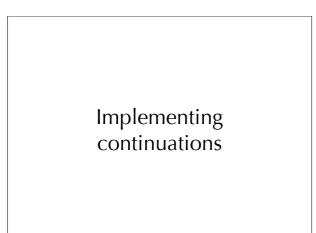
Example: generators Continuations can also be used to implement generators (a.k.a iterators) in the style of Python or C#. Trivial example use: (define ping-pong (generator (lambda (gen) (generator-yield gen "ping") (generator-next ping-pong) ⇒ "ping" (generator-next ping-pong) ⇒ "pong" (generator-next ping-pong) ⇒ "pong"

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GeneratorsA generator is a reference containing alternatively the
continuation of the generator function – when the main
program is executing – and the continuation of the main
program – when the generator function is executing.(define swap-control
(lambda (k-ref val)
(lambda (k)
((ref-swap! k-ref k))
val)))))(define generator-ever gen))))
(define generator-rever
(lambda (gen)
(swap-for-ever gen))))(define swap-control gen #f)
(swap-for-ever gen)))(define generator-next
(lambda (gen)
(swap-control gen #f)
(swap-control gen gen)))

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Implementing call/cc

To implement call/cc, it must be possible to save the current continuation at some point, and restore it later. This can be achieved using two different techniques:

- a low-level technique, which consists in saving and restoring the continuations that are maintained at run time during function calls and returns, and
- a more high-level technique, which consists in transforming the source program to ensure that the current continuation is always explicitly represented as a function, and therefore easy to manipulate.

We will explore both techniques in turn.

Technique #1 Machine continuations

Machine continuations

As explained earlier, all languages have continuations, as they are used to implement function calls:

- · before a function call, the current continuation is saved,
- when a function returns, the most recently saved continuation is resumed.

However, these continuations - that we will call machine $continuations\xspace$ – are usually not first-class values that can be manipulated by the programmer. The aim of call/cc is precisely to turn those continuations into first-class values!

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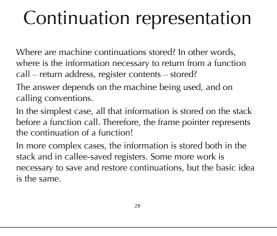
call/cc

Assuming that our language is equipped with two primitives to save and restore machine continuations, call/cc is easy to implement:

(define call/cc

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It remains to be seen how those two primitives can be implemented.



The stack

In a language without first-class continuations, the following two properties are true:

· continuations are saved and resumed in LIFO order,

· continuations can only be resumed once, which implies that they can be freed after having been resumed.

These properties make it possible to use a stack to store continuations. Unfortunately, they do not hold for languages with first-class continuations!

Implementations of such languages either abandon the stack completely and allocate all activation frames on the heap, or lazily copy those frames from the stack to the heap when continuations are saved.

Technique #2 Continuation-passing style

Continuations "by hand"

What can we do if we want to use continuations but the language we use doesn't offer them? One idea is to transform the program to explicitly represent continuations using functions.

- A program is said to be in **continuation-passing style** (**CPS**) if: • all functions receive a continuation as an additional
 - argument, and
 they invoke that continuation with their result instead of returning that result to the caller *i.e.* no function ever returns.

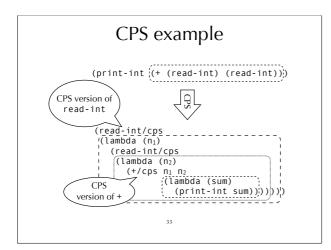
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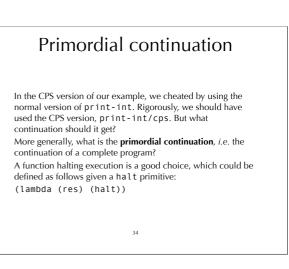
CPS example

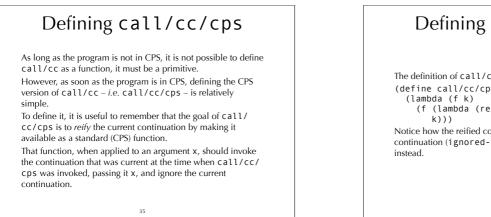
To illustrate CPS, we will use the following simplified variant of our adder program:

(print-int (+ (read-int)) (read-int))) To transform this program to CPS, we need to use functions to represent the current continuation at all possible points of its execution: just after reading the first integer, after reading the second, etc.

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CPS conversion for core minischeme

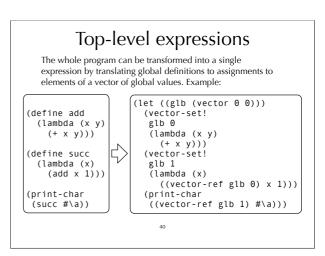
CPS conversion

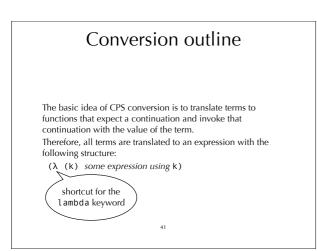
As we have seen, we can offer continuations by first transforming the program to CPS, and then providing an implementation of call/cc/cps. Doing this transformation by hand is tiresome and error-prone, the compiler should do it for us!

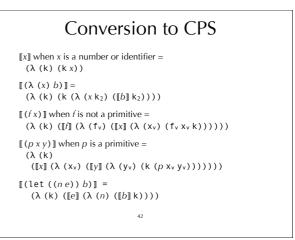
This is the idea of **CPS conversion**, which will be presented here as a function **[**-] mapping (a limited version of) core minischeme terms to equivalent terms in CPS.

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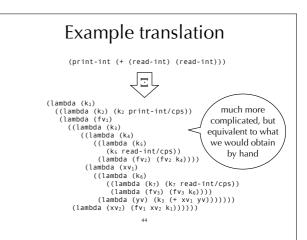
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Conversion to CPS



Administrative redexes	
As the previous example illustrates, the simpl CPS produces a lot of administrative redexes , do not correspond to redexes in the original t One of them is highlighted below:	, <i>i.e.</i> redexes that
<pre>(lambda (k₁) ((lambda (k₂) (k₂ print-int/cps)) (lambda (t₁) ((lambda (k₃)</pre>) -int/cps)))))) yv))))))

