Register allocation

Michel Schinz Advanced Compiler Construction - 2008-05-16

Register allocation

The problem of **register allocation** consists in rewriting a program that makes use of an unbounded number of local variables - also called virtual or pseudo-registers - into one that only makes use of machine registers.

If there are not enough machine registers to store all variables, one or several variables must be spilled, i.e. stored in memory instead of in a register.

Register allocation is generally one of the very last phases of the compilation process - only instruction scheduling can come later. It is performed on an intermediate language that is extremely close to machine code.

Setting the scene

We will illustrate register allocation using programs written in a slight extension of minivm's assembly code:

- apart from *n* machine registers R₀, ..., R_n, an unbounded number of virtual registers $v_{\theta},\,v_{1},\,...$ are available before register allocation,
- machine registers that play a special role, like the frame pointer, are identified with a non-numerical index, e.g. RFP; they are real registers nevertheless,
- a MOVE R_a R_b instruction is available, to copy the contents of R_b into R_a .
- · LOAD and STOR instructions also accept integer values as their third operand, as in LOAD R1 R2 5.

Example function

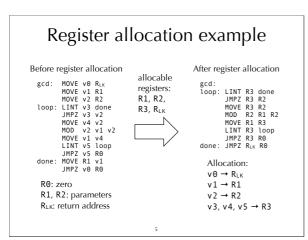
To illustrate register allocation techniques, we will use a function computing the greatest common denominator of two numbers using Euclid's algorithm.

In minischeme

(define gcd (lambda (a b) (if (= 0 b) a a (gcd b (% a b)))))

In (hand	-code	d) a	assembly
gcd:			
	JMPZ	R3	R2
	ADD	R3	R2 R0
	MOD	R2	R1 R2
	ADD	R1	R3 R0
	I TNT	R3	acd

LINT R3 gcd JMPZ R3 R0 done: JMPZ R29 R0



Register allocation techniques

We will study the two most commonly used techniques:

- 1. register allocation by graph colouring, which is relatively slow but produces very good results,
- 2. linear scan register allocation, which is fast but produces slightly worse results - at least in its standard form.

Because it is slow, graph colouring tends to be used in batch compilers, while linear scan tends to be used in JIT compilers

Both techniques are global, i.e. they allocate registers for a whole function at a time.

Technique #1 Register allocation by graph colouring

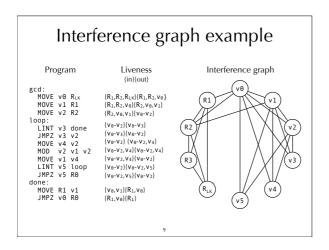
Allocation by graph colouring

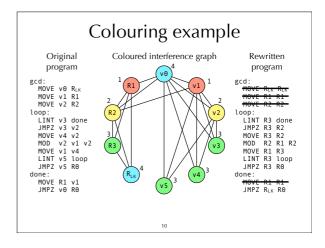
The problem of register allocation can be reduced to the well-known problem of graph colouring, as follows:

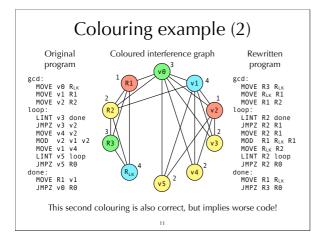
- The interference graph is built. It has one node per register (real or virtual), and two nodes are connected by an edge iff their registers are simultaneously live.
- The interference graph is coloured with at most K colours K = number of available registers so that all nodes have a different colour than all their neighbours.

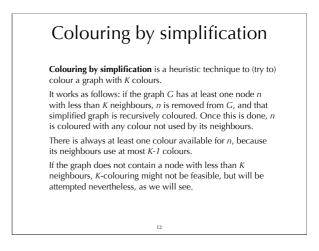
Problems:

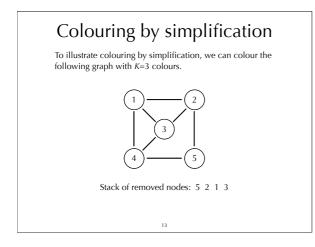
- 1. for an arbitrary graph, the colouring problem is NP-complete,
- 2. a K-colouring might not even exist.

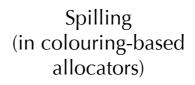












(Optimistic) spilling

During simplification, it is perfectly possible to reach a point where all nodes have at least K neighbours.

When this occurs, a node *n* must be chosen to be **spilled**, *i.e.* have its value stored in memory instead of in a register.

As a first approximation, we assume that the spilled value does not interfere with any other value, remove its node from the graph, and recursively colour the simplified graph as usual.

After the simplified graph has been coloured, it is actually possible that the neighbours of n do not use all the possible colours! In this case, n is not spilled. Otherwise it must really be spilled.

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Spill costs

The node to spill could be chosen at random, but it is clearly better to favour values that are not frequently used, or values that interfere with many others.

The following formula is often used as a measure of the spill cost for a node *n*. The node with the lowest cost should be spilled first.

 $cost(n) = [rw_0 + 10 rw_1 + ... + 10^k rw_k] / degree(n)$ where rw_i is the number of times the value of n is read or written in a loop of depth i, and degree(n) is the number of edges adjacent to n in the interference graph.

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Spilling of pre-coloured nodes

As we have seen, the interference graph contains nodes corresponding to the registers of the machine. These nodes are said to be **pre-coloured**, because the colour of each of them is given by the machine register it represents. Pre-coloured nodes must never be simplified during the colouring process, as by definition they cannot be spilled.

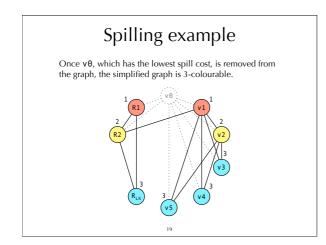
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Spilling example

To illustrate spilling, let's try to colour the same interference graph as before, but with only three colours.

The graph does not contain a node with degree less than three, so the one with the lowest cost must be spilled.

MOVE			node	rw ₀	rw ₁	degree	cost
MOVE MOVE			v0	2	0	7	0.29
DOD:		dono	v1	2	2	6	3.67
JMPZ	v3	v2	v2	1	4	6	6.83
DVE DD		v2 v1 v2	v3	0	2	3	6.67
OVE			v4	0	2	3	6.67
1PZ		loop R0	v 5	0	2	3	6.67
ne: MOVE JMPZ			cost	$= (rw_0)$) + 10	<i>rw</i> 1) / de	egree



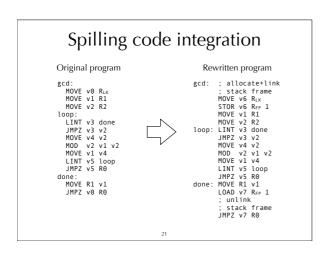
Consequences of spilling

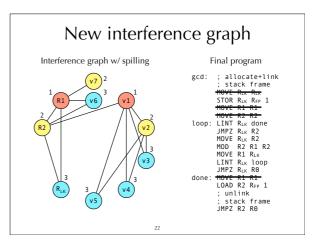
Once a node has been spilled, the original program must be rewritten to take that spilling into account, as follows:

- just before the spilled value is read, code must be inserted to fetch it from memory,
- just after the spilled value is written, code must be inserted to write it back to memory.

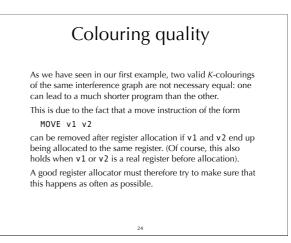
Since that spilling code introduces new virtual registers, the whole register allocation process must be restarted from the beginning.

In practice, one or two iterations are enough in almost all cases.









Coalescing

Given a MOVE instruction of the form

MOVE $v_1 v_2$

and provided that v_1 and v_2 do not interfere, it is always possible to replace all instances of v_1 and v_2 by instances of a new virtual register $v_{1\&2}$. Once this has been done, the MOVE instruction becomes useless and can be removed.

This technique is known as **coalescing**, as the nodes of v_1 and v_2 in the interference graph coalesce into a single node. Coalescing is not always a good idea, though: the coalesced node can have a higher degree than the two original nodes, which might really the graph impariable to experimentially the coalescent k_1 .

node can have a higher degree than the two original nodes, which might make the graph impossible to colour with K colours and require spilling! Some conservatism is required.

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Coalescing heuristics

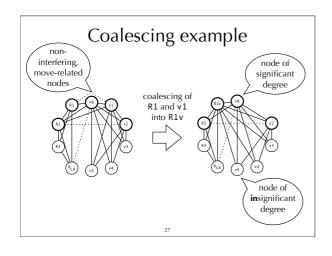
Two coalescing heuristics are commonly used:

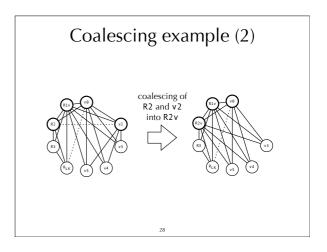
Briggs: coalesce nodes n_1 and n_2 iff the resulting node has less than *K* neighbours of significant degree (*i.e.* of a degree greater or equal to *K*),

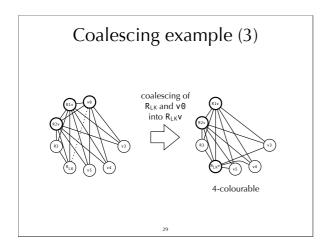
George: coalesce nodes n_1 and n_2 iff all neighbours of n_1 either already interfere with n_2 or are of insignificant degree.

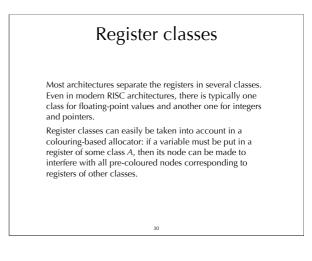
Both heuristics are safe, in that they will not turn a *K*-colourable graph into a non-*K*-colourable one. But they are also conservative, in that they might prevent a coalescing that would be safe.

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Technique #2 Linear scan register allocation

Linear scan

The basic linear scan technique is very simple:

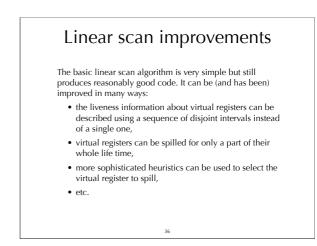
- 1. the program is linearised *i.e.* represented as a linear sequence of instructions, not as a graph,
- a unique live range is computed for every variable, going from the first to the last instruction during which it is live,
- registers are allocated by iterating over the intervals sorted by increasing starting point: each time an interval starts, the next free register is allocated to it, and each time an interval ends, its register is freed,
- 4. if no register is available, the active range ending *last* is chosen to have its variable spilled.

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Discrete and proceedure using close the registers for our gcd procedure using close the registers

	1	2	3	4	5	6	7	8	9	10	11	12
Θ												
1												
2												
3												
4 5												
1												
2												
3												
LК												
ti	me		activ	e inter	vals				alloca	ation		
-	1+ [1	+,12-]					v0→	R3				
_		, -	[1+,12	-]				R3 R3,v1	→R1			
_	2+ [2	+,11-],		-] -],[1+,1	12-]		v0→	R3,v1	→R1 →R1,\	/2→R	2	
	2* [2 3* [3	+,11 ⁻], +,10+],	[2+,11	-		,12 ⁻]	v0→ v0→	R3,v1 R3,v1				• R _{LK}
	2+ [2 3+ [3 4+ [4	*,11*], *,10*], *,5*],[[2 ⁺ ,11 3 ⁺ ,10 ⁺	-],[1+,'	1"],[1*		v0→ v0→ v0→	R3,v1 R3,v1 R3,v1	→R1,\	/2→R	2,v3⊣	

	2	3	4 5	6	7	8	9	10	11	
v0										
/1										
v2 v3		_				_				
/3		-				-	-			
/5										-
R1						-				
R2										
RLK										
time		ctive in	itervals		vA→R		lloca	ition		
1+ [1			itervals		v0→RL v0→RL	ĸ		ition		
1+ [1 2+ [2	,12-]	*,12 ⁻]				к к, v 1 —	•R1		2	
1+ [1 2+ [2 3+ [3	,12] ,11],[1	*,12*] *,11*],[1+,12-]		v0→RL	κ κ,ν1- κ,ν1-	R1	/2→R		LK
1+ [1 2+ [2 3+ [3 4+ [4	,12"] ,11"],[1" ,10"],[2"	*,12 ⁻] *,11 ⁻],[10 ⁺],[2	1+,12-] +,11-]		v0→RL v0→RL	K,V1- K,V1- V1→R	R1 R1,v2	/2→R 2→R2,	v3→R	



Summary

Register allocation is probably the most important compiler optimisation.

Most current compilers allocate registers using one of the following two techniques:

- 1. by transforming the register allocation problem into a graph colouring problem, solved using heuristics,

graph colouring problem, solved using neuristics,
by scanning the live ranges of variables and allocating registers sequentially.
Graph colouring produces the best results but is more complex and slower than the second one. For that reason, graph colouring is usually used in compilers where code quality is more important than compilation speed, and linear scan in the other case.

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