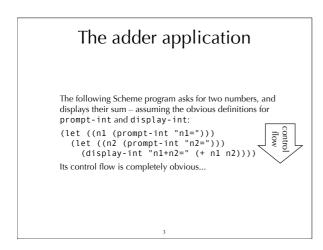
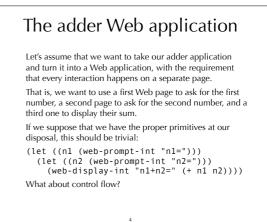
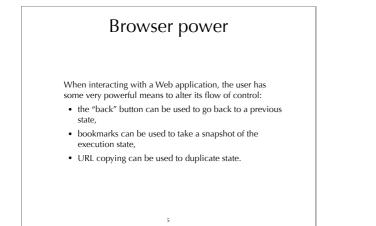
#### Continuations

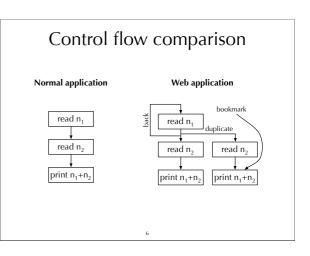
Michel Schinz 2007–05–04

# Control flow of Web applications









#### Solutions for Web applications

Several solutions have been developed to deal with the unusual control flow of Web programs:

- do nothing and let the programmer deal with the complexity *e.g.* PHP,
- tame the browser by disabling both the "back" button and cloning e.g. JWIG,
- use continuations to please the user and the programmer *e.g.* Seaside.

#### Suspended computations

In our adder application, each time some data has to be obtained from the user, the execution of the program is suspended. It is then resumed as soon as the user submits the data.

The power of the Web version of our application comes from the fact that those suspended computations are given a name: the URL associated with them! The user can therefore manipulate those suspended computations at will. She can for example resume the same suspended computation several times, something that is not possible with the non-Web version of the application.

### Continuations

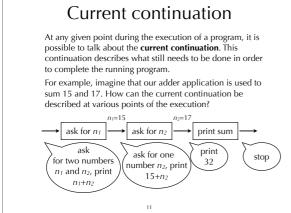
#### Continuations

A **continuation** is a data structure representing a suspended computation.

The main operation that can be performed on a continuation is **resuming** – or **throwing** – it. When a continuation k is resumed, the current execution of the program is *replaced* by the execution of k's computation.

A continuation describes how to continue a suspended computation, hence the name.

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#### Continuations and the Web

In a Web application, execution is suspended each time a page is presented to the user. When the user proceeds – by clicking on a link or by submitting a form – execution is resumed.

In terms of continuations, this means that the current continuation is saved on the server whenever a page is displayed, and associated with a (unique) URL. That saved continuation is resumed later when the user requests its URL.

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#### Functions and continuations

In any programming language, when a function f calls a function g, the execution of f is suspended while g is running, and resumed as soon as g is finished.

In terms of continuations, calling a function therefore consists in saving the current continuation, and then proceed with the execution of the called function. Returning from a function consists in restoring the most recently saved continuation.

In most languages, continuations can only be manipulated in that indirect fashion, through function calls and returns. However, some languages like Scheme offer **first-class continuations**, that is the ability to manipulate continuations like all other values.

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Continuations in Scheme

#### Exposing continuations

How should (first-class) continuations be exposed to the programmer?

In an object-oriented language, continuations could be represented as a class, with methods to obtain the current continuation, or resume an existing continuation.

In a functional language, continuations can be represented as *functions*. Invoking such "continuation functions" resumes the associated continuation. This is how Scheme and several other languages expose continuations.

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#### Continuations in Scheme

Scheme provides the primitive call-with-current-continuation – often abbreviated to call/cc – to obtain the current continuation.

This primitive expects a function as argument, and calls that function with the current continuation as argument, reified as a standard Scheme function.

If that function is invoked later, its continuation will be resumed, and replace the current continuation of the program. Example:

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(call/cc (lambda (k) (k 10) 20))  $\Rightarrow 10$ 

(reified) continuation

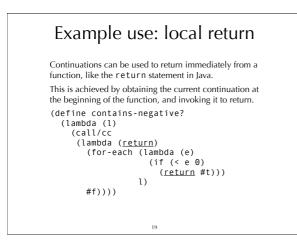
## Understanding call/cc

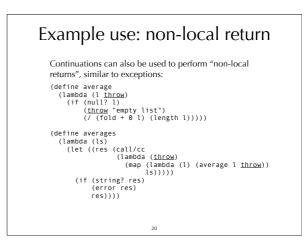
To understand call/cc, it is useful to distinguish two cases:

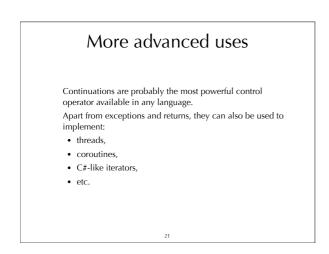
- If the continuation is not invoked, then execution proceeds like if call/cc was not present. Example: (call/cc (lambda (k) (+ 5 6))) ⇒ 11
- 2. If the continuation is invoked with some value v, then execution proceeds like if the call to call/cc returned immediately the value v. Example: (call/cc (lambda (k) (+ (k 5) 6)))  $\Rightarrow$  5

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call/cc examples (call/cc (lambda (k) 10))  $\Rightarrow 10$ (call/cc (lambda (k) (k 10)))  $\Rightarrow 10$ (+ 1 (call/cc (lambda (k) (k 10) 20)))  $\Rightarrow 11$ (call/cc (lambda (k) (k (k (20)))))  $\Rightarrow 20$ (call/cc (lambda (k) (+ (call/cc (lambda (k2) 5)))  $(k_1 6))))$  $\Rightarrow 6$ 







#### Implementing call/cc

To implement call/cc, it must be possible to save the current continuation at some point, and restore it later. This can be achieved using two different techniques:

- a low-level technique, which consists in saving and restoring the continuations that are maintained at run time during function calls and returns, and
- a more high-level technique, which consists in transforming the source program to ensure that the current continuation is always explicitly represented as a function, and therefore easy to manipulate.

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We will explore both techniques in turn.

Technique #1: machine continuations

#### Machine continuations

As explained earlier, all languages have continuations, as they are used to implement function calls:

- before a function call, the current continuation is saved,
- when a function returns, the most recently saved continuation is resumed.

However, these continuations – that we will call **machine continuations** – are usually not first-class values that can be manipulated by the programmer. The aim of call/cc is precisely to turn those continuations into first-class values!

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#### call/cc

Assuming that our language is augmented with two new primitives to save and restore machine continuations, call/cc is easy to implement: (define call/cc (lambda (f) (let ((cc (get-machine-continuation))) (f (lambda (r) (set-machine-continuation! cc) r)))))

It remains to be seen how those two primitives can be implemented.

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#### Continuation representation

Where are machine continuations stored? In other words, where is the information necessary to return from a function call – return address, register contents – stored?

The answer depends on the machine being used, and on calling conventions.

In the simplest case, all that information is stored on the stack before a function call. Therefore, the frame pointer represents the continuation of a function!

In more complex cases, the information is stored both in the stack and in callee-saved registers. Some more work is necessary to save and restore continuations, but the basic idea is the same.

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#### The stack

In a language without first-class continuations, the following two properties are true:

- continuations are saved and resumed in LIFO order,
- continuations can only be resumed once, which implies that they can be freed after having been resumed.

These properties make it possible to use a stack to store continuations. Unfortunately, they do not hold for languages with first-class continuations!

Implementations of such languages either abandon the stack completely and allocate all activation frames on the heap, or lazily copy those frames from the stack to the heap when continuations are saved.

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#### Technique #2: continuation-passing style

#### Continuations "by hand"

What can we do if we want to use continuations but the language we use doesn't offer them?

One idea is to transform the program to explicitly represent continuations using functions.

A program is said to be in **continuation-passing style** (**CPS**) if:

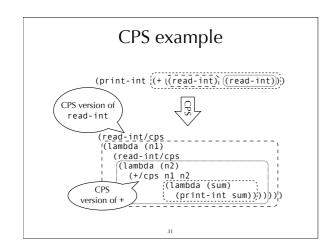
- all functions receive a continuation as an additional argument, and
- they invoke that continuation with their result instead of returning that result to the caller – *i.e.* no function ever returns.

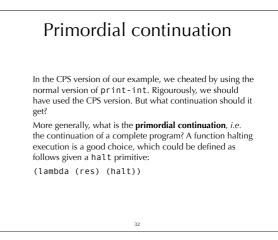
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#### CPS example

To illustrate CPS, we will use the following simplified variant of our adder program:

(print-int (+ (read-int) (read-int))) To transform this program to CPS, we need to use functions to represent the current continuation at all possible points of its execution: just after reading the first integer, after reading the second, etc.





# Defining call/cc/cps

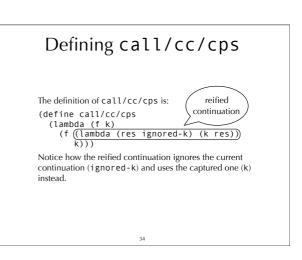
As long as the program is not in CPS, it is not possible to define call/cc, which must be a primitive.

However, as soon as the program is in CPS, defining the CPS version of call/cc - i.e. call/cc/cps - is relatively simple.

To define it, it is useful to remember that the goal of call/ cc/cps is to *reify* the current continuation by making it available as a standard (CPS) function.

That function, when applied to an argument x, should invoke the continuation that was current at the time when call/cc/cps was invoked, passing it x, and ignore the current continuation.

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CPS conversion for minischeme



As we have seen, we can offer continuations by first transforming the program to CPS, and then providing an implementation of call/cc/cps.

Doing this transformation by hand is tiresome and errorprone, the compiler should do it for us!

This is the idea of **CPS conversion**, which will be presented here as a function K mapping minischeme terms to equivalent terms in CPS.

#### Simplified minischeme

To simplify the presentation, we will define CPS conversion for a version of minischeme restricted as follows:

- the body of a lambda expression is composed of a single expression,
- all functions take exactly one argument,
- there is no let expression, as it is only syntactic sugar: (let ((v<sub>1</sub> e<sub>1</sub>) ...) b<sub>1</sub>...)
  - $\Leftrightarrow \text{ ((lambda (v_1 \dots) b_1 \dots) e_1 \dots)}$

Removing those restrictions is relatively easy, and left as an exercise.

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