

SSA Form & Dead Code Elimination Using SSA

Advanced Compiler Techniques
2005
Erik Stenman
Virtutech

Introduction

SSA-form:

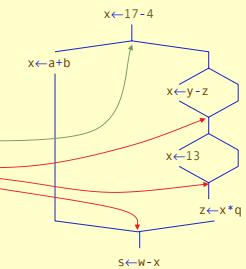
- ♦ Each name is defined exactly once.
- ♦ Each use refers to exactly one name.

What's hard?

- ♦ Straight-line code is trivial.
- ♦ Splits in the CFG are trivial.
- ♦ Joins in the CFG are hard.

Building SSA Form:

- ♦ Insert Φ -functions at birth points.
- ♦ Rename all values for uniqueness.



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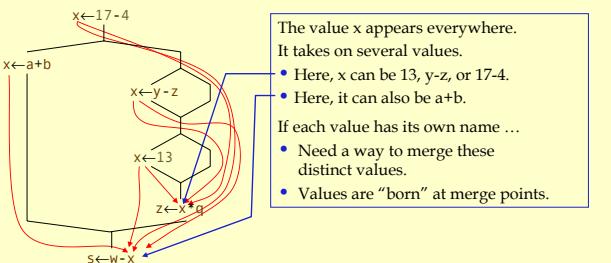
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What is SSA?

Birth Points (*a notion due to Tarjan*)

Consider the flow of values in this example

SSA: Birth Points



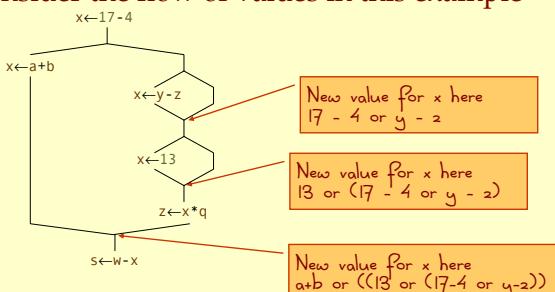
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Birth Points (cont)

Consider the flow of values in this example

SSA: Birth Points



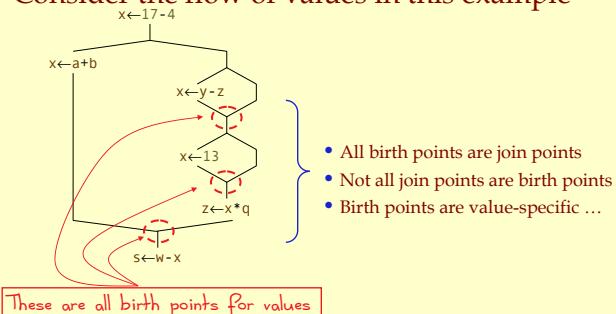
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Birth Points (cont)

Consider the flow of values in this example

SSA: Birth Points



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Static Single Assignment Form

SSA-form:

- ♦ Each name is defined exactly once.
- ♦ Each use refers to exactly one name.

What's hard?

- ♦ Straight-line code is trivial.
- ♦ Splits in the CFG are trivial.
- ♦ Joins in the CFG are hard.

Building SSA Form:

- ♦ Insert Φ -functions at birth points.
- ♦ Rename all values for uniqueness.

A Φ -function is a special kind of copy that selects one of its parameters.

The choice of parameter is governed by the CFG edge along which control reached the current block.

$y_3 \leftarrow \Phi(y_1, y_2)$
However, real machines do not implement a Φ -function in hardware.

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SSA Construction Algorithm (High-level sketch)

1. Insert Φ -functions.
2. Rename values.

... that's all ...

... of course, there is some bookkeeping to be done ...

SSA Construction Algorithm (Less high-level)

1. Insert Φ -functions at every join for every name.
2. Solve *reaching definitions*.
3. Rename each use to the def that reaches it.
(will be unique)

Reaching Definitions

The equations

$$\text{REACHES}(\mathcal{N}_0) = \emptyset$$

$$\text{REACHES}(\mathcal{N}) = \bigcup_{P \in \text{preds}(\mathcal{N})} \text{DEFOUT}(P) \cup (\text{REACHES}(P) \cap \text{SURVIVED}(P))$$

- ♦ $\text{REACHES}(\mathcal{N})$ is the set of definitions that reach block \mathcal{N}
- ♦ $\text{DEFOUT}(\mathcal{N})$ is the set of definitions in \mathcal{N} that reach the end of \mathcal{N}
- ♦ $\text{SURVIVED}(\mathcal{N})$ is the set of definitions not obscured by a new def in \mathcal{N}

Computing $\text{REACHES}(\mathcal{N})$

- ♦ Use any data-flow method (i.e., the iterative method)
- ♦ This particular problem has a very-fast solution (Zadeck)

F.K. Zadeck, "Incremental data-flow analysis in a structured program editor," *Proceedings of the SIGPLAN 84 Conf. on Compiler Construction*, June, 1984, pages 132-143.

SSA Construction Algorithm (Less high-level)

1. Insert Φ -functions at **every join for every name**.
2. Solve *reaching definitions*.
3. Rename each use to the def that reaches it.
(will be unique)

Builds maximal SSA

What's wrong with this approach?

- ♦ Too many Φ -functions. (precision)
- ♦ Too many Φ -functions. (space)
- ♦ Too many Φ -functions. (time)
- ♦ Need to relate edges to Φ -functions parameters. (bookkeeping)

To do better, we need a more complex approach.

SSA Construction Algorithm (Less high-level)

1. Insert Φ -functions

- a.) calculate dominance frontiers
- b.) find global names

for each name, build a list of blocks that define it

- c.) insert Φ -functions

Compute list of blocks where each name is assigned & use as a worklist

\forall global name n
 \forall block B in which n is defined

\forall block D in B 's dominance frontier

insert a Φ -function for n in D
add D to n 's list of defining blocks

This adds to the worklist!

Creates the iterated dominance frontier

Use a checklist to avoid putting blocks on the worklist twice;
keep another checklist to avoid inserting the same Φ -function twice.

2. Rename variables in a pre-order walk over dominator tree

(use an array of stacks, one stack per global name)

Staring with the root block, B

- a.) generate unique names for each Φ -function and push them on the appropriate stacks

1 counter per name for subscripts

- b.) rewrite each operation in the block

- i. Rewrite uses of global names with the current version (from the stack)

- ii. Rewrite definition by inventing & pushing new name

- c.) fill in Φ -function parameters of successor blocks

- d.) recurse on B 's children in the dominator tree

- e.) on exit from block B pop names generated in B from stacks

Need the end-of-block name for this path

Reset the state

Aside on Terminology: Dominators

Definitions

- \mathcal{X} dominates \mathcal{Y} if and only if every path from the entry of the control-flow graph to the node for \mathcal{Y} includes \mathcal{X}
- By definition, \mathcal{X} dominates \mathcal{X}
- We associate a set of dominators (Dom) with each node
- $|\text{Dom}(\mathcal{X})| \geq 1$

Immediate dominators

- For any node \mathcal{X} , there must be a \mathcal{Y} in $\text{Dom}(\mathcal{X})$ closest to \mathcal{X}
- We call this \mathcal{Y} the immediate dominator of \mathcal{X}
- As a matter of notation, we write this as $\text{IDom}(\mathcal{X})$

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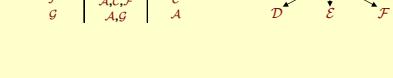
Dominators (cont)

Dominators have many uses in program analysis & transformation:

- Finding loops.
- Building SSA form.
- Making code motion decisions.

Dominator sets

Block	Dom	IDom
A	A	-
B	A,B	A
C	A,C	A
D	A,C,D	C
E	A,C,E	C
F	A,C,F	C
G	A,G	A



Let's look at how to compute dominators...

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SSA Construction Algorithm (Low-level detail)

Computing Dominance

- First step in Φ -function insertion computes dominance.
- A node \mathcal{N} dominates \mathcal{M} iff \mathcal{N} is on every path from \mathcal{N}_0 to \mathcal{M}
 - Every node dominates itself
 - \mathcal{N} 's immediate dominator is its closest dominator, $\text{IDom}(\mathcal{N})^\dagger$

$$\text{DOM}(\mathcal{N}_0) = \{\mathcal{N}_0\}$$

Initially, $\text{Dom}(n) = \mathcal{N}, \forall n \neq n_0$

$$\text{DOM}(\mathcal{N}) = \{\mathcal{N}\} \cup (\cap_{P \in \text{preds}(\mathcal{N})} \text{DOM}(P))$$

Computing DOM

- These equations form a rapid data-flow framework
- Iterative algorithm will solve them in $d(G) + 3$ passes
 - Each pass does $|\mathcal{N}|$ unions & $|\mathcal{E}|$ intersections,
 - \mathcal{E} is $O(N^2) \Rightarrow O(N^2)$ work

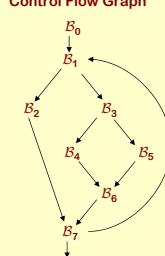
$d(G)$ is the loop-connectedness of the graph w.r.t a DFST
 • Maximal number of back edges in an acyclic path.
 • Several studies suggest that, in practice, $d(G)$ is small, (< 3)
 • For most CFGs, $d(G)$ is independent of the specific DFST.

[†] $\text{IDom}(\mathcal{N}) \neq \mathcal{N}$, unless \mathcal{N} is \mathcal{N}_0 , by convention.

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Example

Control Flow Graph



Progress of iterative solution for DOM

Iteration	Dom(n)							
	0	1	2	3	4	5	6	7
0	0	N	N	N	N	N	N	N
1	0	0,1	0,1,2	0,1,3	0,1,3,4	0,1,3,5	0,1,3,6	0,1,7
2	0	0,1	0,1,2	0,1,3	0,1,3,4	0,1,3,5	0,1,3,6	0,1,7

Results of iterative solution for Dom & IDom

Iteration	Dom(n)							
	0	1	2	3	4	5	6	7
Dom	0	0,1	0,1,2	0,1,3	0,1,3,4	0,1,3,5	0,1,3,6	0,1,7
IDom	0	0	1	1	3	3	3	1

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Example

Progress of iterative solution for DOM

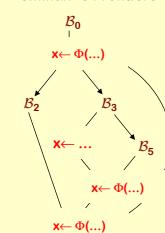
Iteration	Dom(n)							
	0	1	2	3	4	5	6	7
0	0	N	N	N	N	N	N	N
1	0	0,1	0,1,2	0,1,3	0,1,3,4	0,1,3,5	0,1,3,6	0,1,7
2	0	0,1	0,1,2	0,1,3	0,1,3,4	0,1,3,5	0,1,3,6	0,1,7

Results of iterative solution for Dom & IDom

Iteration	Dom(n)							
	0	1	2	3	4	5	6	7
Dom	0	0,1	0,1,2	0,1,3	0,1,3,4	0,1,3,5	0,1,3,6	0,1,7
IDom	0	0	1	1	3	3	3	1

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Dominance Frontiers



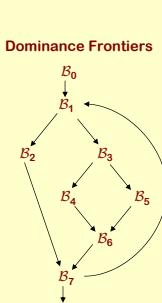
Example

Dominance Frontiers & Φ -Function Insertion

- A definition at \mathcal{N} forces a Φ -function at \mathcal{M} iff $\mathcal{N} \notin \text{Dom}(\mathcal{M})$ but $\mathcal{N} \in \text{Dom}(\mathcal{P})$ for some $\mathcal{P} \in \text{preds}(\mathcal{M})$
- $\text{DF}(\mathcal{V})$ is the fringe just beyond the region that \mathcal{V} dominates.
- $\text{DF}(B_4)$ is $\{B_6\}$, so \leftarrow in B_4 forces a Φ -function in B_6
- \leftarrow in B_6 forces a Φ -function in $\text{DF}(B_6) = \{B_7\}$
- \leftarrow in B_7 forces a Φ -function in $\text{DF}(B_7) = \{B_1\}$
- \leftarrow in B_1 forces a Φ -function in $\text{DF}(B_1) = \emptyset$ (halt)

For each assignment, we insert the Φ -functions

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Example

Computing Dominance Frontiers

- Only join points are in $DF(\mathcal{V})$ for some \mathcal{N}
- Leads to a simple, intuitive algorithm for computing dominance frontiers
 - For each join point \mathcal{M} (i.e., $|preds(\mathcal{M})| > 1$)
 - For each CFG predecessor of \mathcal{M}
 - Run up to $IDOM(\mathcal{M})$ in the dominator tree, adding \mathcal{M} to $DF(\mathcal{V})$ for each \mathcal{N} between \mathcal{M} and $IDOM(\mathcal{M})$
- For some applications, we need post-dominance, the post-dominator tree, and reverse dominance frontiers, $RDF(\mathcal{V})$
 - Just dominance on the reverse CFG
 - Reverse the edges & add unique exit node
- We will use these in dead code elimination

SSA Construction Algorithm (Reminder)

- Insert Φ -functions at every join for every name

a.) calculate dominance frontiers

b.) find global names

Needs a little more detail
for each name, build a list of blocks that define it

c.) insert Φ -functions

\forall global name n

\forall block B in which n is defined

\forall block D in B 's dominance frontier

insert a Φ -function for n in D

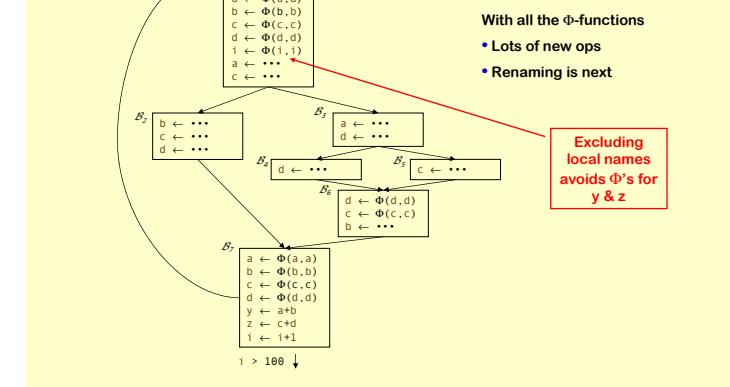
add D to n 's list of defining blocks

SSA Construction Algorithm

Finding global names

- Different between two forms of SSA
- Minimal uses all names
- Semi-pruned SSA uses names that are live on entry to some block
 - Shrinks name space & number of Φ -functions
 - Pays for itself in compile-time speed
- For each "global name", need a list of blocks where it is defined
 - Drives Φ -function insertion
 - B defines x implies a Φ -function for x in every $C \in DF(B)$

Pruned SSA adds a test to see if x is live at insertion point



SSA Construction Algorithm (Less high-level)

- Rename variables in a pre-order walk over dominator tree (use an array of stacks, one stack per global name)

Starting with the root block, B

- generate unique names for each Φ -function and push them on the appropriate stacks
- rewrite each operation in the block
 - Rewrite uses of global names with the current version (from the stack)
 - Rewrite definition by inventing & pushing new name
- fill in Φ -function parameters of successor blocks
- recurse on B 's children in the dominator tree
- <on exit from block B > pop names generated in B from stacks

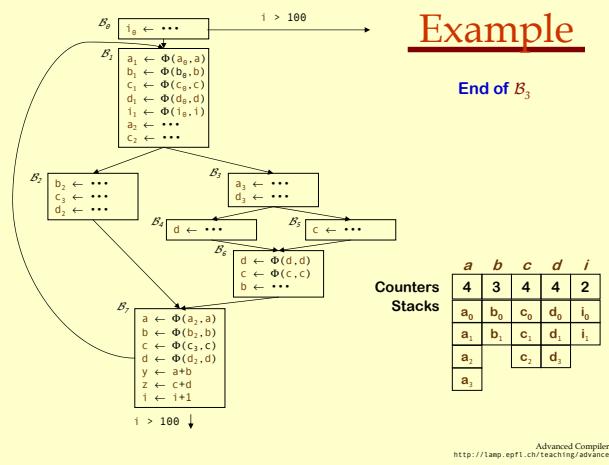
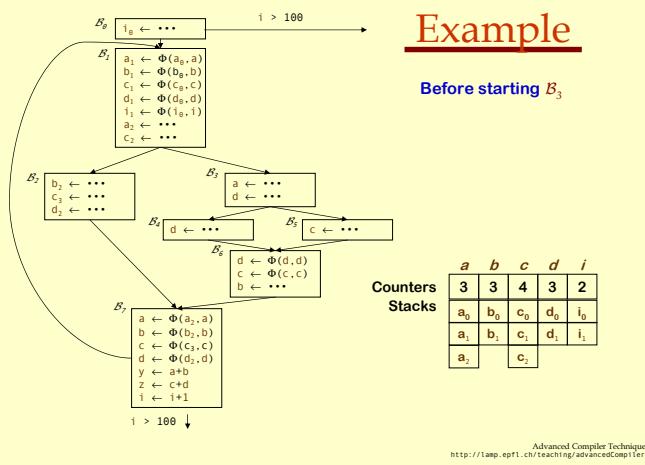
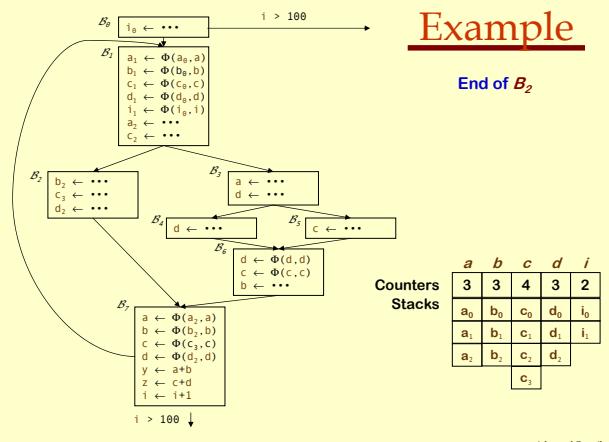
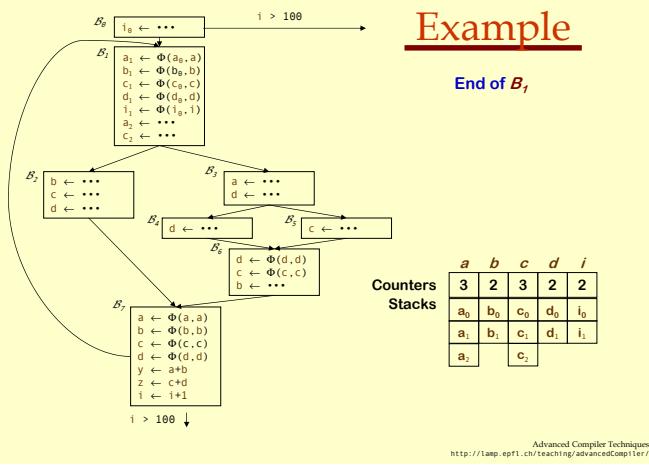
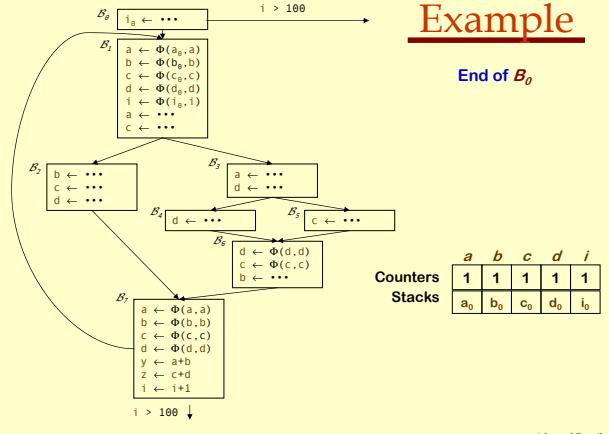
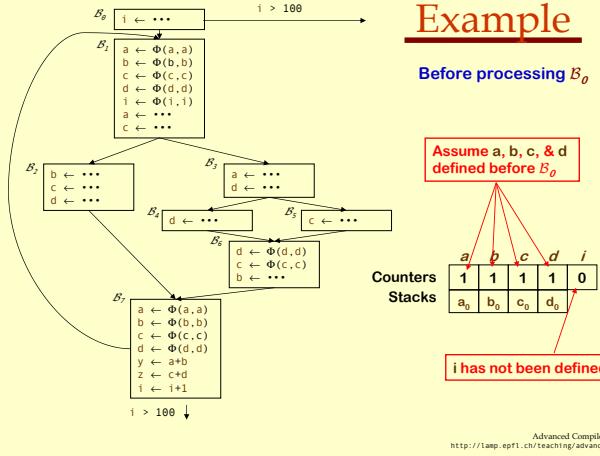
SSA Construction Algorithm (Less high-level)

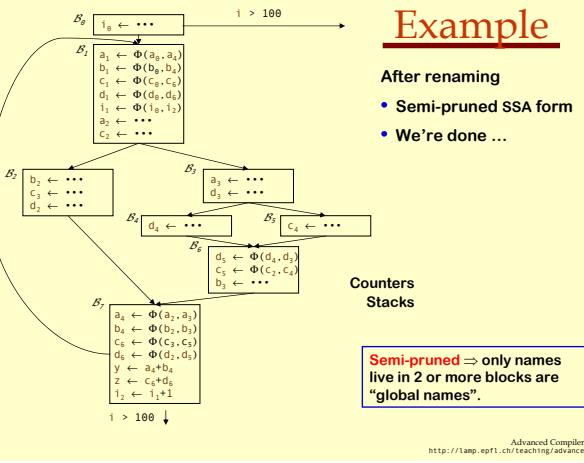
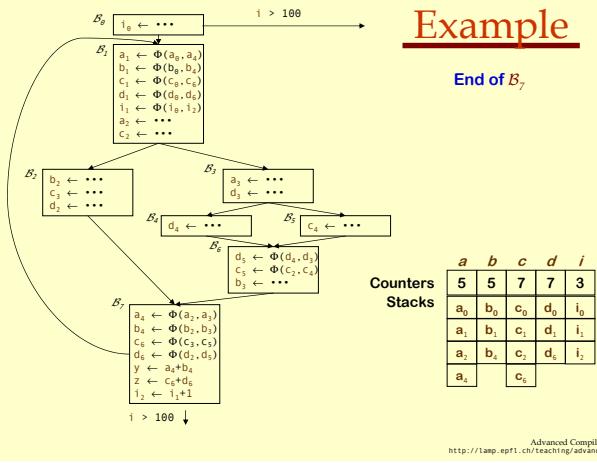
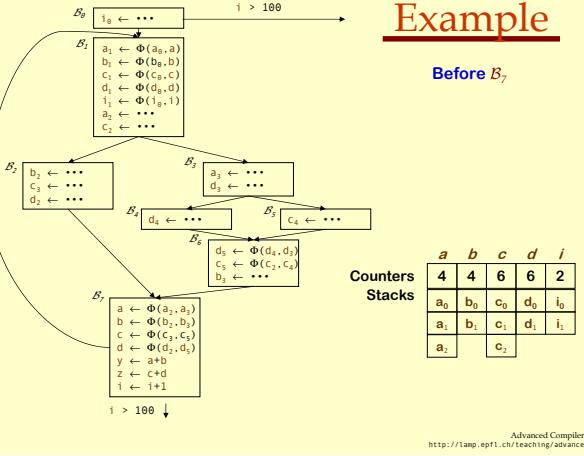
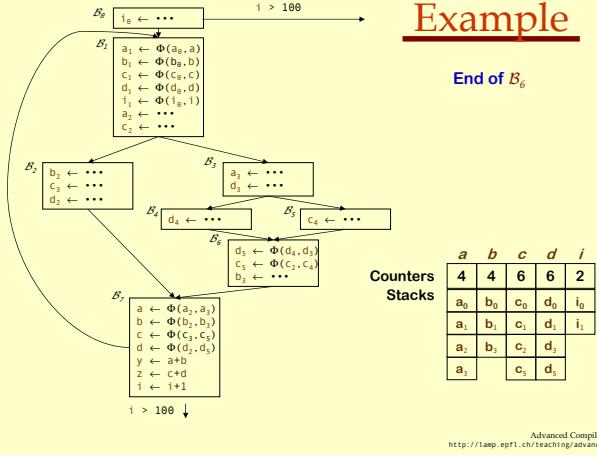
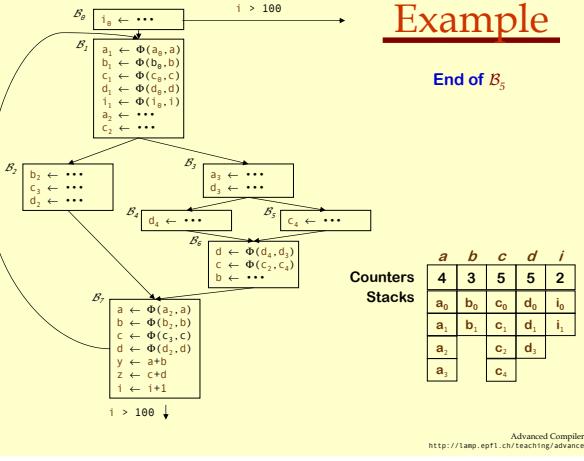
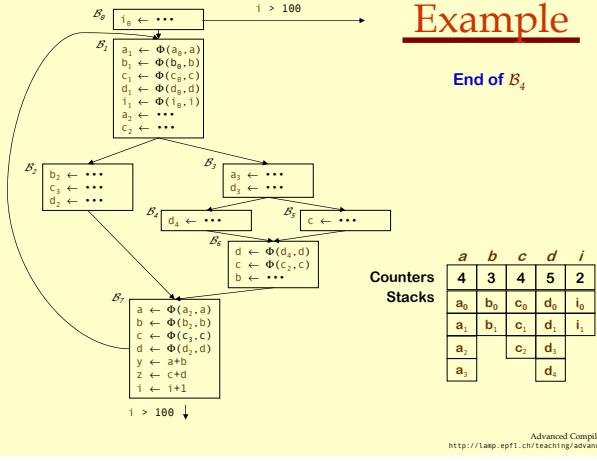
Adding all the details ...

```
for each global name i
  counter[i] ← 0
  stack[i] ← ∅
  call Rename( $B_0$ )
```

```
NewName(v)
  i ← counter[v]
  counter[v] ← counter[v] + 1
  push v_i onto stack[v]
  return v_i
```

```
Rename(B)
  for each  $\Phi$ -function in  $B$ ,  $x \leftarrow \Phi(\dots)$ 
    rename  $x$  as NewName( $x$ )
  for each operation " $x \leftarrow y \text{ op } z$ " in  $B$ 
    rewrite  $y$  as  $top(stack[y])$ 
    rewrite  $z$  as  $top(stack[z])$ 
    rewrite  $x$  as NewName( $x$ )
  for each successor of  $B$  in the CFG
    rewrite appropriate  $\Phi$  parameters
  for each successor  $S$  of  $B$  in dom. tree
    Rename( $S$ )
  for each operation " $x \leftarrow y \text{ op } z$ " in  $B$ 
    pop(stack[x])
```





SSA Construction Algorithm (Pruned SSA)

What's this "pruned SSA" stuff?

- ♦ Minimal SSA still contains extraneous Φ -functions.
- ♦ Inserts some Φ -functions where they are dead.
- ♦ Would like to avoid inserting them.

Two ideas

- ♦ **Semi-pruned SSA:** discard names used in only one block.
 - ♦ Significant reduction in total number of Φ -functions.
 - ♦ Needs only local liveness information.
- ♦ **Pruned SSA:** only insert Φ -functions where their value is live.
 - ♦ Inserts even fewer Φ -functions, but costs more to do.
 - ♦ Requires global live variable analysis.

(cheap to compute)

(more expensive)

In practice, both are simple modifications to step 1.

SSA Construction Algorithm

We can improve the stack management.

- ♦ Push at most one name per stack per block. (save push & pop)
- ♦ Thread names together by block.
- ♦ To pop names for block B , use B 's thread.

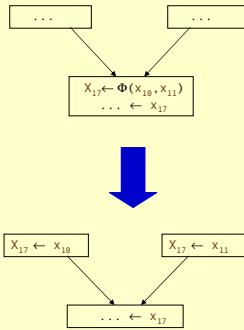
This is a good use for a scoped hash table.

- ♦ Significant reductions in pops and pushes.
- ♦ Makes a minor difference in SSA construction time.
- ♦ Scoped table is a clean, clear way to handle the problem.

SSA Deconstruction

At some point, we need executable code.

- ♦ Few machines implement Φ operations.
- ♦ Need to fix up the flow of values.



Dead Code Elimination Using SSA

Dead code elimination

- ♦ Conceptually similar to mark-sweep garbage collection:
- ♦ Mark useful operations.
- ♦ Everything not marked is useless.
- ♦ Need an efficient way to find and to mark useful operations.
- ♦ Start with critical operations.
- ♦ Work back up SSA edges to find their antecedents.
- ♦ Operations defined as critical:
 - ♦ I/O statements,
 - ♦ linkage code (*entry & exit blocks*),
 - ♦ return values,
 - ♦ calls to other procedures.

Algorithm will use post-dominators & reverse dominance frontiers.

Dead Code Elimination Using SSA

```
Mark
for each op i
  clear i's mark
  if i is critical then
    mark i
    add i to WorkList

while (WorkList ≠ ∅)
  remove i from WorkList
  if i has form "x ← y op z"
    if def(y) is not marked then
      mark def(y)
      add def(y) to WorkList
    if def(z) is not marked then
      mark def(z)
      add def(z) to WorkList

  for each b ∈ RDF(block(i))
    mark the block-ending
    branch in b
    add it to WorkList
```

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

- Notes:
- Eliminates some branches.
 - Reconnects dead branches to the remaining live code.
 - Find useful post-dominator by walking post-dominator tree.
 > Entry & exit nodes are useful

Dead Code Elimination Using SSA

Handling Branches

- ♦ When is a branch useful?
- ♦ When another useful operation depends on its existence

In the CFG, j is control dependent on i if

1. \exists a non-null path p from i to j such that j post-dominates every node on p after i
2. j does not strictly post-dominate i

- ♦ j control dependent on $i \Rightarrow$ one path from i leads to j , one doesn't
- ♦ This is the reverse dominance frontier of j ($RDF(j)$)

Algorithm uses $RDF(n)$ to mark branches as live

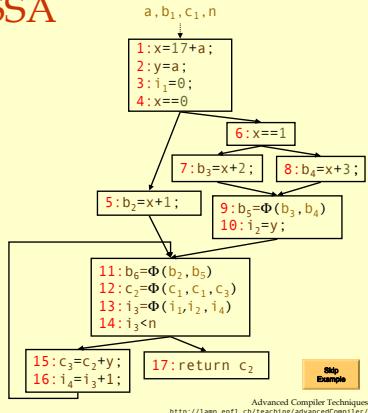
Dead Code Elimination Using SSA

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for each op i
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if i is critical then
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while (Worklist ≠ ∅)
remove i from WorkList
(i has form "x←y op z")
if def(y) is not marked then
mark def(y)
add def(y) to WorkList
if def(z) is not marked then
mark def(z)
add def(z) to WorkList
for each b ∈ RDF(block(i))
mark the block-ending
branch in b
add it to WorkList

```

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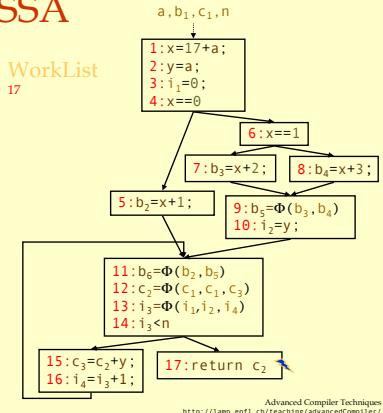
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clear i's mark
if i is critical then
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add i to WorkList

while (Worklist ≠ ∅)
remove i from WorkList
(i has form "x←y op z")
if def(y) is not marked then
mark def(y)
add def(y) to WorkList
if def(z) is not marked then
mark def(z)
add def(z) to WorkList
for each b ∈ RDF(block(i))
mark the block-ending
branch in b
add it to WorkList

```

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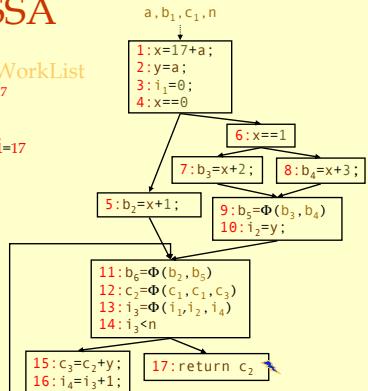
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for each op i
clear i's mark
if i is critical then
mark i
add i to WorkList

while (Worklist ≠ ∅)
remove i from WorkList
(i has form "op z")

if def(z) is not marked then
mark def(z)
add def(z) to WorkList
for each b ∈ RDF(block(i))
mark the block-ending
branch in b
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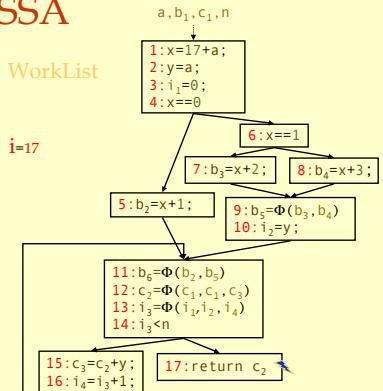
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(i has form "op z")

if def(z) is not marked then
mark def(z)
add def(z) to WorkList
for each b ∈ RDF(block(i))
mark the block-ending
branch in b
add it to WorkList

```

Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination Using SSA

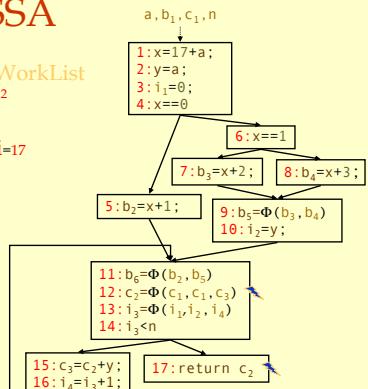
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for each op i
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Advanced Compiler Techniques
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Dead Code Elimination Using SSA

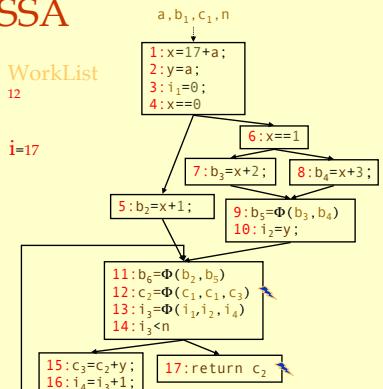
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Advanced Compiler Techniques
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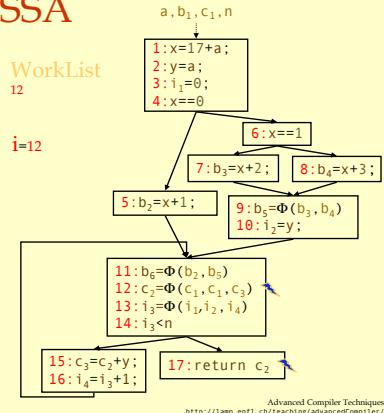
Dead Code Elimination Using SSA

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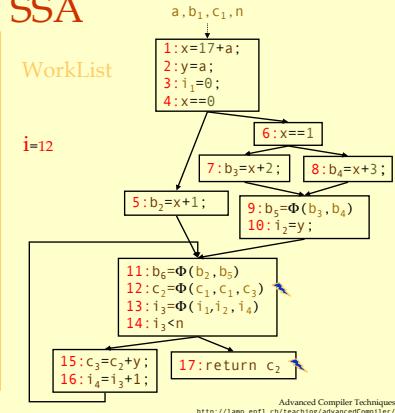
Dead Code Elimination Using SSA

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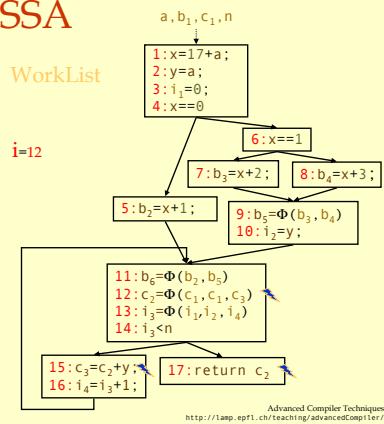
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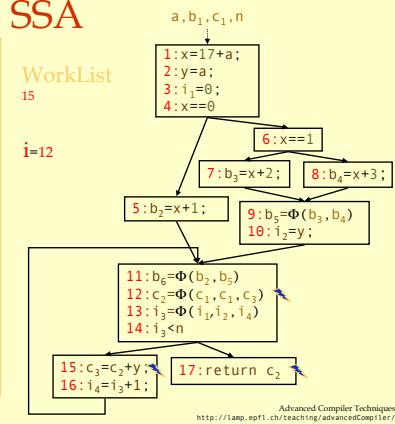
Dead Code Elimination Using SSA

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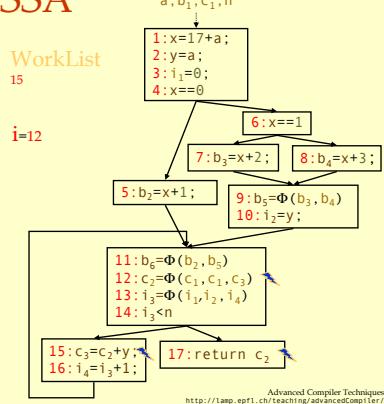
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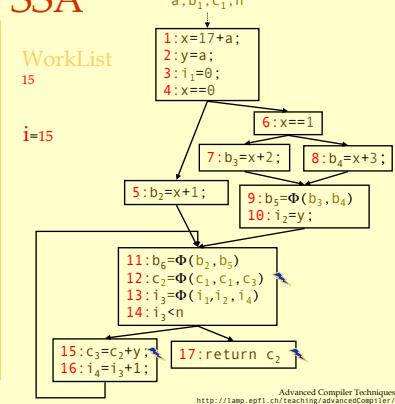
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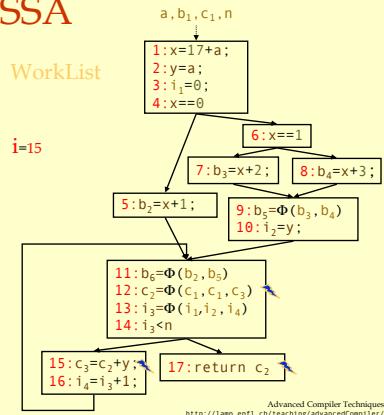
Dead Code Elimination Using SSA

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<http://lamp.epfl.ch/teaching/advancedCompiler/>

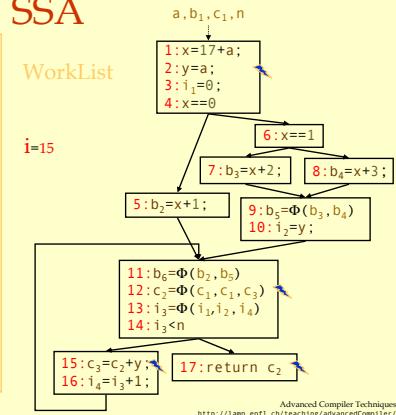
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<http://lamp.epfl.ch/teaching/advancedCompiler/>

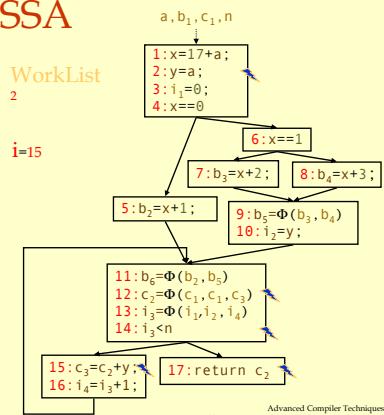
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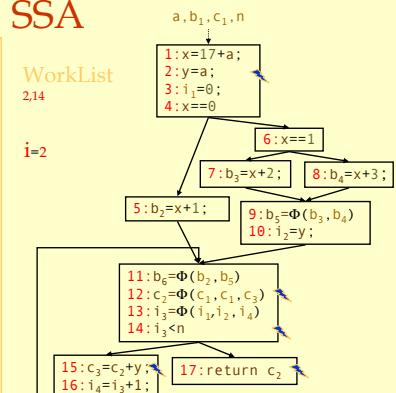
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<http://lamp.epfl.ch/teaching/advancedCompiler/>

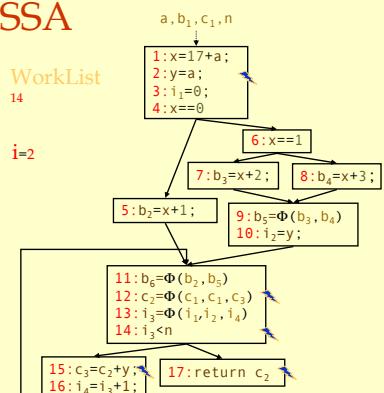
Dead Code Elimination Using SSA

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<http://lamp.epfl.ch/teaching/advancedCompiler/>

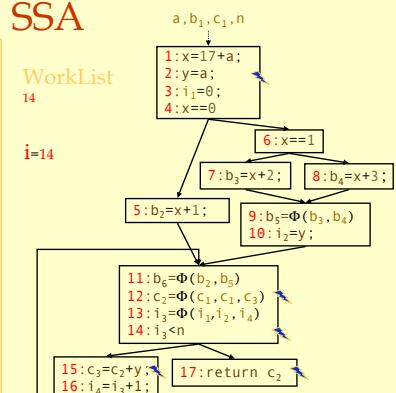
Dead Code Elimination Using SSA

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<http://lamp.epfl.ch/teaching/advancedCompiler/>

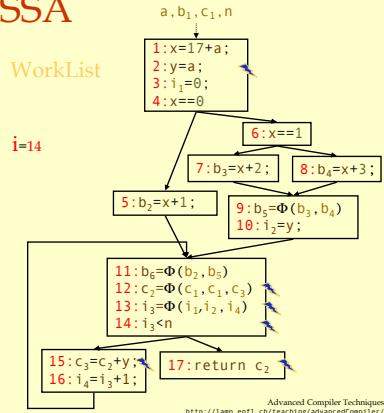
Dead Code Elimination Using SSA

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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

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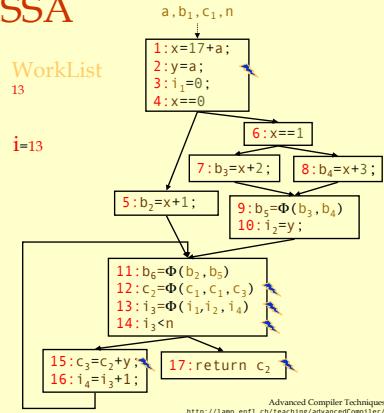
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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

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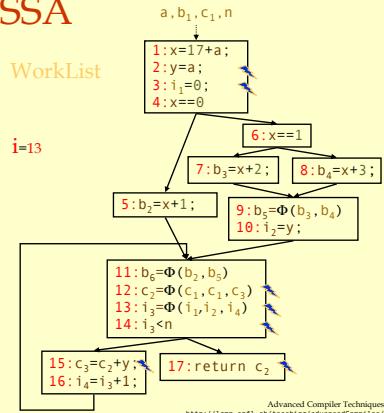
Dead Code Elimination Using SSA

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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

63

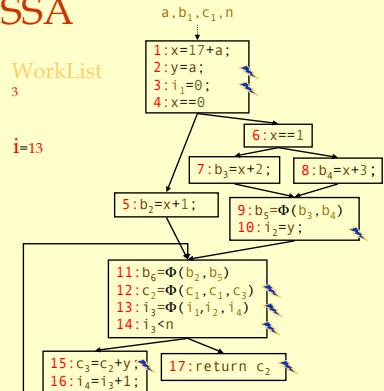
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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

64

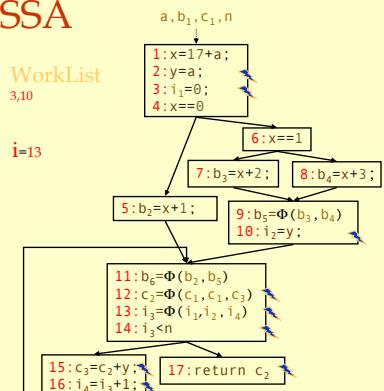
Dead Code Elimination Using SSA

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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

65

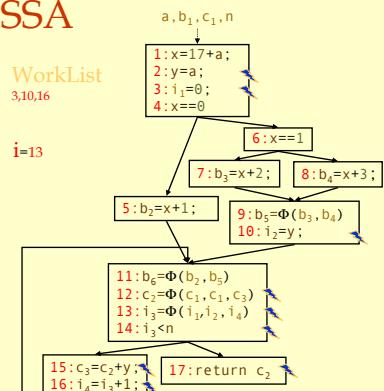
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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

66

Dead Code Elimination Using SSA

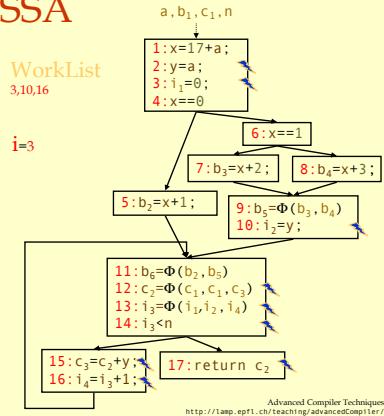
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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

67

Dead Code Elimination Using SSA

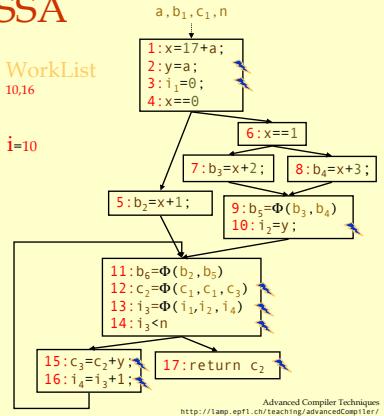
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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

68

Dead Code Elimination Using SSA

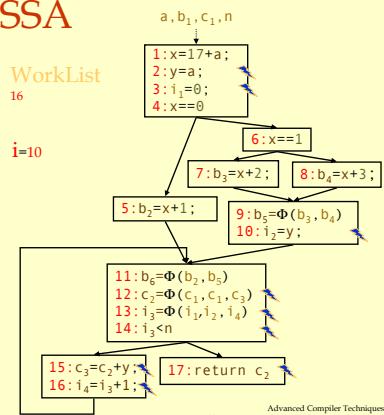
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Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

69

Dead Code Elimination Using SSA

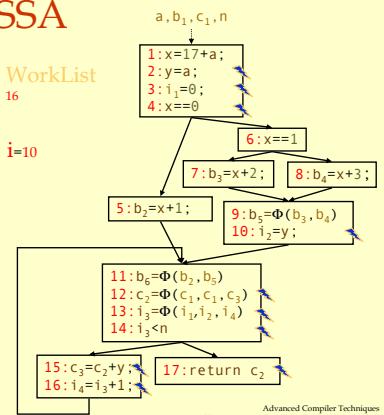
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Advanced Compiler Techniques
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Dead Code Elimination

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Dead Code Elimination Using SSA

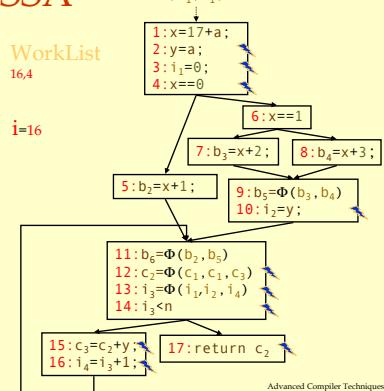
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Advanced Compiler Techniques
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Dead Code Elimination

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Dead Code Elimination Using SSA

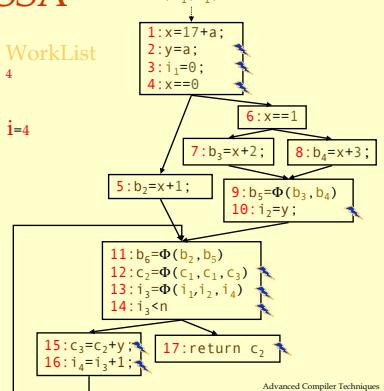
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Advanced Compiler Techniques
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Dead Code Elimination

72

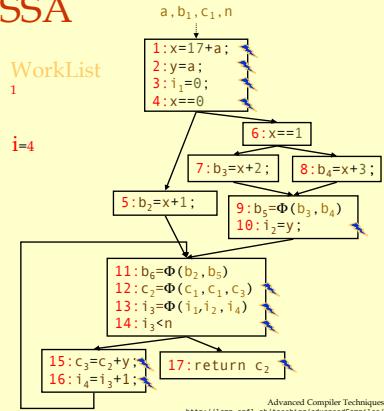
Dead Code Elimination Using SSA

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Advanced Compiler Techniques
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Dead Code Elimination

73

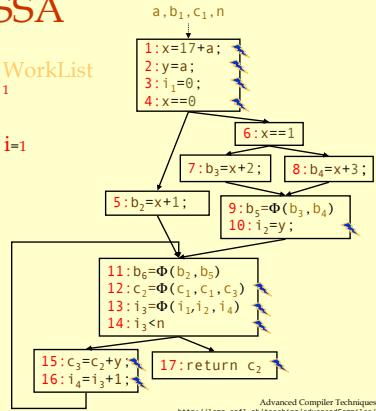
Dead Code Elimination Using SSA

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Advanced Compiler Techniques
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Dead Code Elimination

74

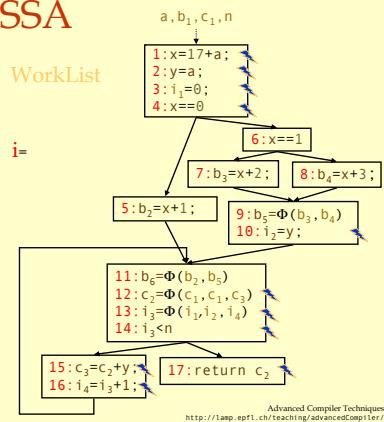
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if def(z) is not marked then
mark def(z)
add def(z) to WorkList
for each b ∈ RDF(block(i))
mark the block-ending
branch in b
add it to WorkList

```



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

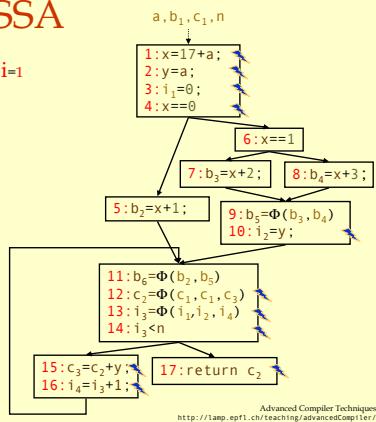
75

Dead Code Elimination Using SSA

```

Sweep
for each op i
if i is not marked then
if i is a branch then
rewrite with a jump to
i's nearest useful
post-dominator
if i is not a jump then
delete i

```



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

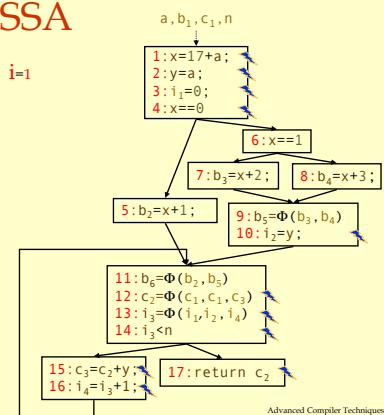
76

Dead Code Elimination Using SSA

```

Sweep
for each op i
if i is not marked then
if i is a branch then
rewrite with a jump to
i's nearest useful
post-dominator
if i is not a jump then
delete i

```



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

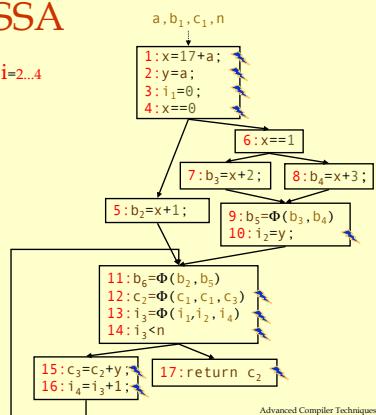
77

Dead Code Elimination Using SSA

```

Sweep
for each op i
if i is not marked then
if i is a branch then
rewrite with a jump to
i's nearest useful
post-dominator
if i is not a jump then
delete i

```



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

Dead Code Elimination

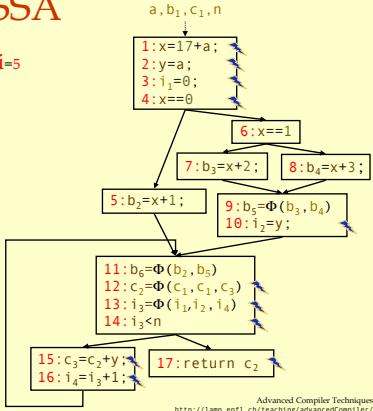
78

Dead Code Elimination Using SSA

Dead Code Elimination

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

i=5



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

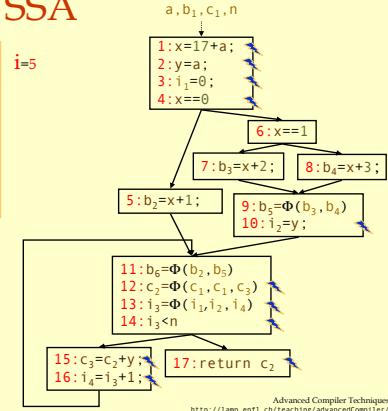
79

Dead Code Elimination Using SSA

Dead Code Elimination

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

i=5



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

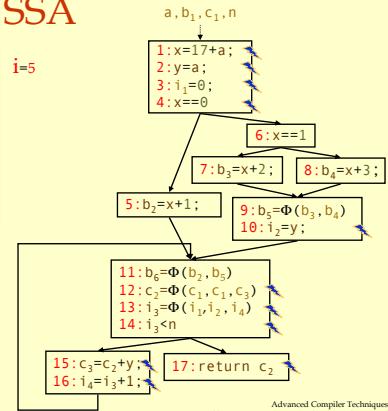
80

Dead Code Elimination Using SSA

Dead Code Elimination

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

i=5



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

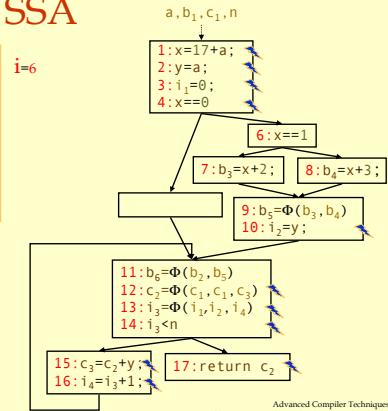
81

Dead Code Elimination Using SSA

Dead Code Elimination

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

i=6



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

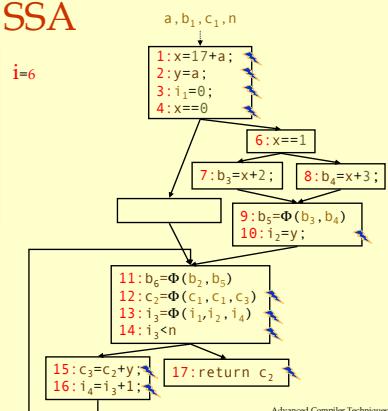
82

Dead Code Elimination Using SSA

Dead Code Elimination

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

i=6



Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

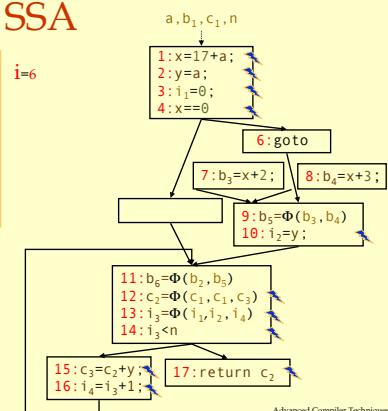
83

Dead Code Elimination Using SSA

Dead Code Elimination

```
Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
```

i=6



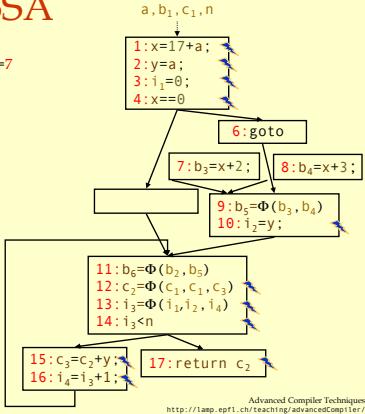
Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

84

Dead Code Elimination Using SSA

```

Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
  
```

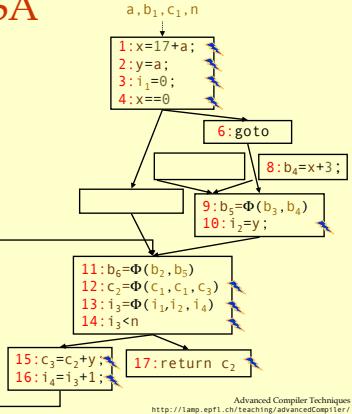
i=7Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

85

Dead Code Elimination Using SSA

```

Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
  
```

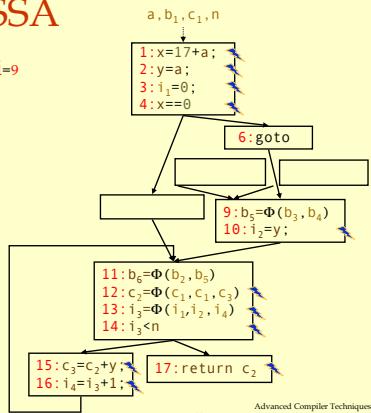
i=8Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

86

Dead Code Elimination Using SSA

```

Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
  
```

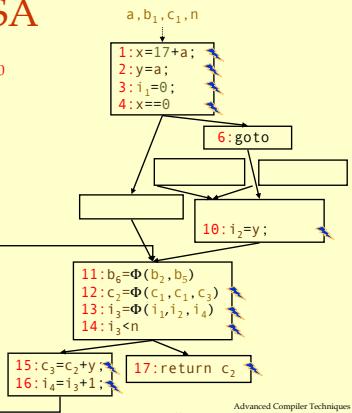
i=9Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

87

Dead Code Elimination Using SSA

```

Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
  
```

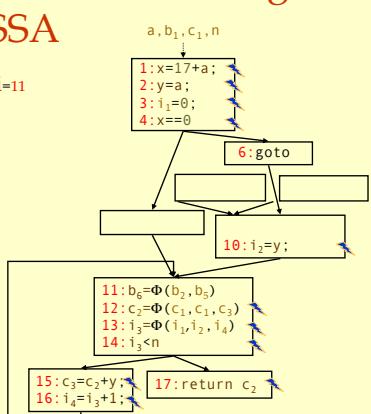
i=10Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

88

Dead Code Elimination Using SSA

```

Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
  
```

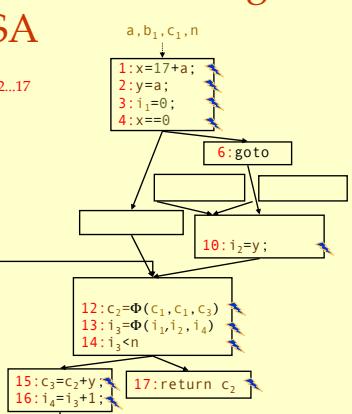
i=11Advanced Compiler Techniques
<http://lamp.epfl.ch/teaching/advancedCompiler/>

89

Dead Code Elimination Using SSA

```

Sweep
for each op i
  if i is not marked then
    if i is a branch then
      rewrite with a jump to
      i's nearest useful
      post-dominator
    if i is not a jump then
      delete i
  
```

i=12..17Advanced Compiler Techniques
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90

Dead Code Elimination Using SSA

What's left?

- ◆ Algorithm eliminates useless definitions & some useless branches
- ◆ Algorithm leaves behind empty blocks & extraneous control-flow

Algorithm from: Cytron, Ferrante, Rosen, Wegman, & Zadeck, *Efficiently Computing Static Single Assignment Form and the Control Dependence Graph*, ACM TOPLAS 13(4), October 1991

with a correction due to Rob Shillner

Two more issues

- ◆ Simplifying control-flow
- ◆ Eliminating unreachable blocks

Both are CFG transformations (no need for SSA)