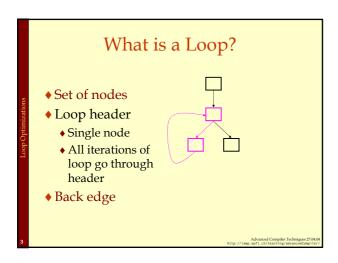
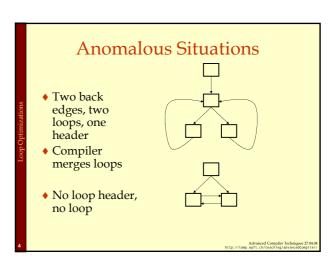


Loop Optimizations

- ◆ Important because lots of execution time occurs in loops
- ♦ First, we will identify loops
- ♦ We will study three optimizations
 - ◆ Loop-invariant code motion
 - ◆ Strength reduction
 - Induction variable elimination

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Defining Loops With Dominators

Recall the concept of *dominators*:

- ◆ Node n dominates a node m if all paths from the start node to m go through n.
- ◆ The *immediate dominator* of m is the last dominator of m on any path from start node.
- A *dominator tree* is a tree rooted at the start node:
 - Nodes are nodes of control flow graph.
 - ullet Edge from d to n if d is the immediate dominator of n.

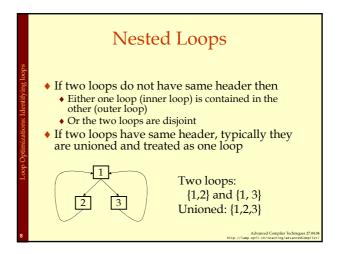
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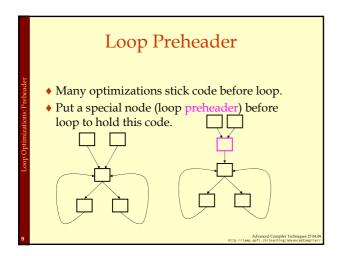
Identifying Loops

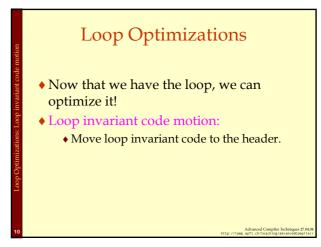
- A loop has a unique entry point the header.
- ♦ At least one path back to header.
- Find edges whose heads (>) dominate tails (-), these edges are back edges of loops.
- ◆ Given a back edge n→d:
 - ◆ The node d is the loop header.
 - The loop consists of n plus all nodes that can reach n without going through d (all nodes "between" d and n)

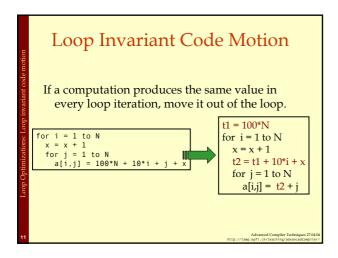
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Loop Construction Algorithm loop(d,n) $loop = \emptyset; stack = \emptyset; insert(n);$ while stack not empty do m = pop stack; $for all p \in pred(m) do insert(p);$ insert(m) $if m \notin loop then$ $loop = loop \cup \{m\};$ push m onto stack;









Detecting Loop Invariant Code • A statement is loop-invariant if operands are • Constant, • Have all reaching definitions outside loop, or • Have exactly one reaching definition, and that definition comes from an invariant statement • Concept of exit node of loop • node with successors outside loop

Loop Invariant Code Detection Algorithm

for all statements in loop

if operands are constant or have all reaching definitions outside loop, mark statement as invariant

do

for all statements in loop not already marked invariant if operands are constant, have all reaching definitions outside loop, or have exactly one reaching definition from invariant statement

then mark statement as invariant until there are no more invariant statements

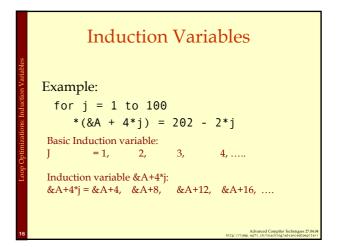
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Loop Invariant Code Motion

- ◆ Conditions for moving a statement s: x = y+z into loop header:
 - s dominates all exit nodes of loop
 - If it does not, some use after loop might get wrong value
 Alternate condition: definition of x from s reaches no use outside loop (but moving s may increase run time)
 - \bullet No other statement in loop assigns to \boldsymbol{x}
 - ♦ If one does, assignments might get reordered
 - No use of x in loop is reached by definition other than s
 - $\ensuremath{\blacklozenge}$ If one is, movement may change value read by use

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Order of Statements in Preheader Preserve data dependences from original program (can use order in which discovered by algorithm) $\begin{array}{c} b = 2 \\ i = 0 \end{array}$ $\begin{array}{c} a = b * b \\ c = a + a \end{array}$ $\begin{array}{c} i = i + c \end{array}$ Advanced Compiler Techniques 2724AM nttp://lame.efft.co// teaching/pate-acceled compiler.



What are induction variables?

- ◆ x is an *induction variable* of a loop L if
 - variable changes its value every iteration of the loop
 - the value is a function of number of iterations of the loop
- In programs, this function is normally a linear function

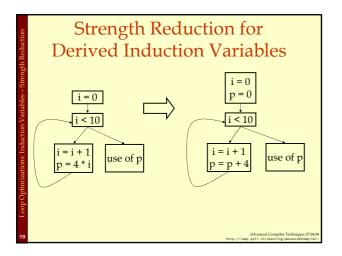
Example: for loop index variable j, function d + c*j

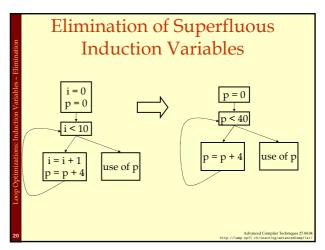
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Types of Induction Variables

- Base induction variable:
- Only assignments in loop are of form $i = i \pm c$
- Derived induction variables:
 - Value is a linear function of a base induction variable.
 - Within loop, j = c*i + d, where i is a base induction variable
 - Very common in array index expressions an access to a[i] produces code like p = a + 4*i.

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Three Algorithms

- Detection of induction variables:
 - Find base induction variables.
 - Each base induction variable has a family of derived induction variables, each of which is a linear function of base induction variable.
- Strength reduction for derived induction variables.
- Elimination of superfluous induction variables.

Output of Induction Variable Detection Algorithm

- Set of induction variables:
 - base induction variables.
 - derived induction variables.
- ♦ For each induction variable j, a triple <i,c,d>:
 - ♦ i is a base induction variable.
 - ♦ the value of j is i*c+d.
 - ♦ j belongs to family of i.

Induction Variable Detection Algorithm

Scan loop to find all base induction variables

Scan loop to find all variables k with one assignment of form k = j*b where j is an induction variable with triple

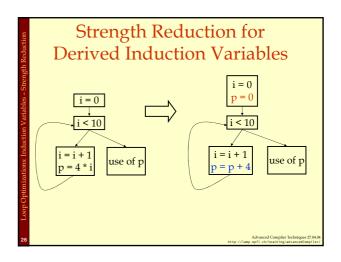
make k an induction variable with triple <i,c*b,d*b> Scan loop to find all variables k with one assignment of form $k = j\pm b$ where j is an induction variable with triple

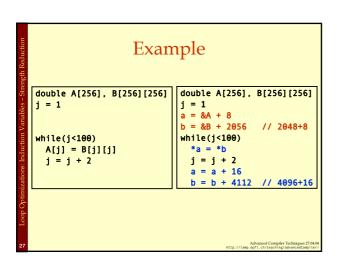
make k an induction variable with triple <i,c,b±d> until no more induction variables are found

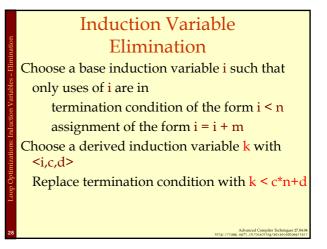
Strength Reduction

```
t = 202
for j = 1 to 100
  t = t - 2
  *(abase + 4*j) = t
Basic Induction variable:
         = 1, 1, 2, 1, 3, 1, 4, ....
Induction variable 202 - 2*j
t = 202, 200, 198, 196, ....
Induction variable abase+4*j:
abase+4*j = abase+4, abase+8, abase+12, abase+16, ....
```

Strength Reduction Algorithm for all derived induction variables j with triple $\langle i,c,d \rangle$ Create a new variable sReplace assignment $j=i^*c+d$ with j=sImmediately after each assignment i=i+e, insert statement $s=s+c^*e$ (c^*e is constant) place s in family of i with triple $\langle i,c,d \rangle$ Insert $s=c^*i+d$ into preheader







Summary Loop Optimization Important because lots of time is spent in loops. Detecting loops. Loop invariant code motion. Induction variable analyses and optimizations: Strength reduction. Induction variable elimination.